A Novel Approach for Mining High-Utility Sequential Patterns in Sequence Databases

Chowdhury Farhan Ahmed, Syed Khairuzzaman Tanbeer, and Byeong-Soo Jeong

I. Introduction

Mining sequential patterns is an important research issue in data mining and knowledge discovery with broad applications. However, the existing sequential pattern mining approaches consider only binary frequency values of items in sequences and equal importance/significance values of distinct items. Therefore, they are not applicable to actually represent many real-world scenarios. In this paper, we propose a novel framework for mining high-utility sequential patterns for more real-life applicable information extraction from sequence databases with non-binary frequency values of items in sequences and different importance/significance values for distinct items. Moreover, for mining high-utility sequential patterns, we propose two new algorithms: UtilityLevel is a high-utility sequential pattern mining with a level-wise candidate generation approach, and UtilitySpan is a high-utility sequential pattern mining with a pattern growth approach. Extensive performance analyses show that our algorithms are very efficient and scalable for mining high-utility sequential patterns.

Keywords: Data mining, sequential patterns, high-utility patterns, knowledge discovery.
transaction databases, where the order of elements in a pattern is not maintained. The existing model considers non-binary frequency values of items in transactions and different profit values of items in contrast to the assumption of binary frequency values of items in transactions and equal importance/significance values of items in the traditional frequent pattern mining model [14]-[16]. It uses a measure called “utility” to overcome the limitations of the support measure. This utility measure calculates the actual profit value of a pattern in a transaction database. The problem of HUP mining refers to find out those patterns having utility value greater than or equal to a user-given minimum threshold with respect to the transaction database. By using this measure, very important and useful patterns can be discovered which may not be possible with the support measure. For example, the support measure may not be able to detect a pattern such as gold ring, gold necklace because this pattern may have very small support value. On the other hand, a utility measure can easily discover this pattern because it considers the profit value as well as the non-binary frequency value. By utility mining, several important business area decisions like maximizing revenue, minimizing marketing, and/or inventory costs can be considered, and knowledge about itemsets/customers contributing to the majority of the profit can be discovered. In addition to the real-world retail market, other application areas, such as stock tickers, network traffic measurements, web-server logs, data feeds from sensor networks, and telecommunications call records can have similar solutions.

Motivated by the above real-life scenarios, in this paper, we propose a novel framework for mining high-utility sequential patterns. Our framework considers both internal and external utilities of a sequence and introduces a new measure, sequence utility (SeqUtility), to calculate the utility value of a sequence. It also defines the high-utility sequential patterns and the problem of mining high-utility sequential patterns. Moreover, we propose two new algorithms for mining high-utility sequential patterns: UtilityLevel (UL) is a high-utility sequential pattern mining with a level-wise candidate generation approach, and UtilitySpan (US) is a high-utility sequential pattern mining with a pattern growth approach. The first algorithm, UL, is simple and straightforward compared to the second algorithm. However, it adopts a level-wise candidate generation-and-test mechanism [1], [2]. Hence, it generates a large number of candidate sequences and needs several database scans. On the other hand, the second algorithm, US, exploits a sequential pattern growth mining approach [5], [6] and successfully avoids the problems of the UL algorithm. It needs a maximum of three database scans. Accordingly, it significantly reduces the number of candidate sequences as well as the overall runtime for mining high-utility sequential patterns. Extensive performance analyses show that our algorithms are very efficient for mining high-utility sequential patterns.

The remainder of this paper is organized as follows. In section II, we describe related work. In section III, we propose our framework. In section IV, we develop our proposed algorithms for mining high-utility sequential patterns. In section V, our experimental results are presented and analyzed. Finally, in section VI, conclusions are drawn.

II. Related Work

1. HUP Mining

The theoretical model and definitions of HUP mining were given in [8]. This approach is called mining with expected utility. Later, the same authors proposed two new algorithms, UMining and UMining_H, to calculate HUPs [9]. However, these methods do not satisfy the “downward closure” property of Apriori [14] and overestimate too many patterns. This property says that if a pattern is infrequent, then all of its super-patterns must be infrequent. The Two-Phase [10] algorithm was developed based on the definitions of [8] for HUP mining using the downward closure property with a measure called “transaction-weighted utilization.” The isolated items discarding strategy (IIDS) [12] for discovering HUPs was proposed to reduce some candidates in every pass of databases. Applying IIDS, the authors developed two efficient HUP mining algorithms: FUM and DCG+. However, these algorithms suffer from the problem of level-wise candidate generation-and-test methodology and need several database scans. An efficient candidate pruning technique, HUC-Prune [11], has been proposed to avoid the level-wise candidate generation-and-test problem in HUP mining. In [13], efficient tree structures have been proposed for incremental HUP mining. However, these approaches are not applicable for mining high-utility sequential patterns.

2. Sequential Pattern Mining

The sequential pattern mining problem was first introduced by Agrawal and Srikant in [1]. They have designed Apriori-based algorithms to mine all the sequential patterns according to a user-given minimum threshold. Later, an improved algorithm, generalized sequential pattern [2], was proposed for sequential pattern mining. Zaki [3] devised an algorithm which is a sequential pattern discovery using equivalent classes (SPADE). SPADE was developed for sequential pattern mining using vertical data format. These algorithms are based on the level-wise candidate generation-and-testing
mechanism and generate too many candidate patterns. The SPAM algorithm [4] uses a depth-first search strategy using an efficient vertical bitmap representation. An efficient algorithm, PrefixSpan [5], [6], was proposed by using a sequential pattern growth mining approach. The BIDE algorithm [7] can efficiently discover closed sequential patterns without candidate maintenance.

Research has been done for sequential pattern mining with constraints. The SPIRIT algorithm [17] has been developed for mining sequential patterns with user-specified regular expression constraints. Pei and others [18] developed a new framework, Prefix-growth, for different types of constraint-based sequential pattern mining including item, length, super-pattern, aggregate, regular expression, duration, and gap constraints. Some algorithms have also been developed to handle weight and quantity constraints in sequential pattern mining. The WSpan [19] and WIS [20] algorithms use different weight values for different items, but cannot consider non-binary frequency values of items. Kim and others [21] proposed two algorithms: Apriori-QSP and PrefixSpan-QSP. These were created by extending the existing Apriori-style and PrefixSpan algorithms of traditional sequential pattern mining, respectively. They have also proposed two improved versions of these algorithms, Apriori-All and PrefixSpan-All [21]. However, the SQUIRE approach cannot consider items with different weights/profits. Moreover, it is based on the support measure. For example, if a sequence is \{3, 2, 1\}, then it just finds its support in the SDB, that is, in how many TSSs it is present. As a consequence, none of the existing approaches are capable of mining high-utility sequences. Therefore, in this paper, we propose a novel framework and two new algorithms for mining high-utility sequential patterns in SDBs.

III. Proposed Framework

Let \( I = \{i_1, i_2, \ldots, i_q\} \) be a set of items and \( P = \{p_1, p_2, \ldots, p_r\} \) be a pattern (itemset), where \( P \subseteq I \) and \( I \subseteq \{1, n\} \). A sequence \( S \) is denoted by \( \{s_1, s_2, \ldots, s_r\} \), an ordered list of patterns, that is, each \( s_q \) (1 \( \leq q \leq r \)) is a pattern \( P \), and each pattern appearing in a sequence is called an element of the sequence. The length of a sequence is the number of instances of items inside it. Consider there are two sequences, for example, \( \alpha = \{a_1, a_2, \ldots, a_x\} \) and \( \beta = \{b_1, b_2, \ldots, b_y\} \) (\( \alpha \leq y \)). If there exists \( j_1 < j_2 < \cdots < j_x \leq y \), such that \( a_1 \subseteq b_{j_1}, a_2 \subseteq b_{j_2}, \ldots, a_x \subseteq b_{j_x} \), then \( \alpha \) is a subsequence of \( \beta \), and \( \beta \) is a super-sequence of \( \alpha \). An SDB contains a number of TSSs: \( \{TS_1, TS_2, \ldots, TS_m\} \). \( TS_k \) (1 \( \leq k \leq m \)) contains a tuple \( \langle \text{SID}_k, S_k \rangle \), where \( \text{SID}_k \) is the sequence ID, and \( S_k \) is the sequence of the \( TS_k \). \( TS_k \) is said to contain a sequence, \( X \), if \( X \) is a subsequence of \( S_k \).

**Definition 1.** The internal utility value of an item, \( i_j \), in \( TS_k \) is represented by \( \text{iu}(i_j, S_k) \). External utility \( \text{eu}(i_j) \) is the impact/significance value of item \( i_j \). Figure 1 shows an example SDB with internal and external utility values. Here, the internal utility values represent the quantities of items in sequences, and the external utility value of each item represents profit ($) per unit of that item. For example, in Fig. 1, \( \text{iu}(b, S_1) = 6 \), and \( \text{eu}(b) = 7 \). However, an item may appear multiple times in a TS. In that case, \( \text{iu}(i_j, S_k) \) is the addition of all the quantities of \( i_j \) in sequence \( S_k \). For example, in Fig. 1, \( \text{iu}(a, S_1) = 10 \).

**Definition 2.** Sequence utility, \( su(i_j, S_k) \), is the quantitative measure of utility for item \( i_j \) in \( TS_k \), defined by

\[
su(i_j, S_k) = \text{iu}(i_j, S_k) \times \text{eu}(i_j).
\]

For example, \( su(b, S_1) = 6 \times 7 = 42 \) in Fig. 1.

**Definition 3.** A sequence, for example, \( X = \{x_1, x_2, \ldots, x_m\} \), is called an \( m \)-sequence, where \( X \subseteq S_k, x_i \subseteq I \), and \( 1 \leq i \leq m \). To calculate the internal utility of an item, \( i_j \), in a sequence \( X \) (\( X \subseteq S_k \)), we have to take only the internal utility of \( i_j \) in \( X \). For example, \( \text{iu}(d, de(abh), S_3) = 2 \) (where \( X = de(abh) \)). Hence, as with an item, a sequence \( X \) may have multiple distinct occurrences in \( TS_k \). Accordingly, for sequence utility of \( X \) in \( S_k \), \( su(X, S_k) \) is defined by

\[
su(X, S_k) = \sum_{\forall X \subseteq S_k} \sum_{i \in X} su(i, X, S_k) \).
\]

However, in the above equation, we refer to only all distinct occurrences of \( X \). For example, sequence \( de \) has two distinct occurrences in \( S_k \). Hence, \( su(de, S_k) = (2 \times 10 + 1 \times 6) + (3 \times 10 + 3 \times 6) + (26 \times 48) = 74 \) in Fig. 1. If multiple distinct occurrences cannot be formed, then a sequence is formed by taking the maximum \( su \) of a sequence. For example, in the \( S_k \) sequence, \( eb \) can be formed by taking the fourth \( b \) or the sixth \( b \). Here, the fourth item \( b \) is taken as it gives the maximum \( su \) of \( eb \) in \( S_k \).
Definition 4. The sequence utility of $TS_k$ is defined by
\[ su(TS_k) = \sum_{i \in S_k} su(i, S_k). \] (3)

For example, $su(TS_1) = su(a, S_1)+su(b, S_1)+su(d, S_1)+su(f, S_1) = 50 + 42 + 30 + 8 = 130$.

Definition 5. The sequence utility of a sequence $X$ in an SDB is defined by
\[ su(X, SDB) = \sum_{TSD \in SDB} \sum_{X \subseteq TSD} su(X, S). \] (4)

For example, $su(a(b)d\alpha, SDB) = su(a(b)d\alpha, TS_3) + su(a(b)d\alpha, TS_4) = 102 + 129 = 231$ in Fig. 1.

Definition 6. The sequence utility value of an SDB is defined by
\[ su(SDB) = \sum_{TS_k \subseteq SDB} su(TS_k). \] (5)

For example, $su(SDB) = 743$ in Fig. 1.

Definition 7. The minimum sequence utility threshold, $\delta$, is given by the percentage of sequence utility value of the database. In Fig. 1, if $\delta$ is 30% or can be expressed as 0.3, then the minimum sequence utility value can be defined as
\[ minSeqUtil = \delta \times su(SDB). \] (6)

Hence, in this example, $minSeqUtil = 0.3 \times 743 = 223$ in Fig. 1.

Definition 8. A sequence $X$ is a high-utility sequential pattern if $su(X) \geq minSeqUtil$. Mining high-utility sequential pattern means discovering all the sequences $X$ having criteria $su(X) \geq minSeqUtil$. For $minSeqUtil = 223$, $a(b)d\alpha$ is a high-utility sequential pattern as $su(a(b)d\alpha) = 231$.

The most challenging problem for high-utility sequential pattern mining is that sequence utilities do not have the downward closure property. Consider $minSeqUtil = 223$ in Fig. 1: $a$ is a low-utility sequential pattern as $su(a) = 135$, but its super-sequence $a(b)d\alpha$ is a high-utility sequential pattern as $su(a(b)d\alpha) = 231$. Therefore, the downward closure property is not satisfied. To maintain the downward closure property in high-utility sequential pattern mining, we define a new measure called sequence-weighted utility (swu).

Definition 9. The swu value of a sequence $X$ is defined by
\[ swu(X) = \sum_{X \subseteq S_k \subseteq SDB} su(TS_k). \] (7)

Definition 10. $X$ is a high-swu sequence if $swu(X) \geq minSeqUtil$.

As it is the maximum possible sequence utility value of a sequence, the downward closure property can be maintained by using this value. For example, $swu(g) = su(TS_3) = 67$ in Fig. 1. Here, for $minSeqUtil = 223$ in Fig. 1, as $swu(g) < minSeqUtil$, any super-sequence of $g$ cannot be a high-swu sequence and obviously cannot be a high-utility sequential pattern. In our approach, after finding all the high-swu sequence maintaining the downward closure property, we calculate all the high-utility sequential patterns form high-swu sequences.

Lemma 1. The swu value of a sequence $X$ maintains the downward closure property.

Proof. Let $X$ be a high-swu sequence and $SDB_k$ is the set of sequences containing $X$. Let $Y$ be a superset of $X$, then $Y$ cannot be present in any sequence where $X$ is absent. Therefore, according to definition 9, the maximum swu value of $Y$ is $swu(X)$. Accordingly, if $swu(X)$ is less than $minSeqUtil$, $Y$ cannot be a high-swu sequence.

Lemma 2. For an SDB and minimum sequence utility threshold, the set of high-utility sequential patterns ($S$) is a subset of the set of high-swu sequences ($WS$).

Proof. Let $X$ be a high-utility sequential pattern. According to definitions 5 and 9, $su(X)$ must be less than or equal to $swu(X)$. So, if $X$ is a high-utility sequential pattern, it must be a high-swu sequence. Hence, $X$ is a member of the set $WS$ and $S \subseteq WS$.

IV. Mining High-Utility Sequential Patterns

1. UL Algorithm

Our first proposed algorithm, UL, is simple and straightforward. It is used for generating high-utility sequential patterns. It adopts a level-wise candidate generation approach for mining high-utility sequential patterns. At first, it generates the candidates for high-swu sequences, and subsequently generates high-swu sequences (actual candidates for high-utility sequential patterns). Finally, it detects the high-utility sequential patterns from high-swu sequences.

The level-by-level candidate generation-and-testing mechanism is shown in Table 1 for the SDB presented in Fig. 1 and $minSeqUtil = 30\%$. In level-1, all the distinct items are candidate length-1 high-swu sequences. The UL algorithm scans the SDB once to generate all the length-1 high-swu sequences. In level-2, 51 candidate high-swu sequences are generated as shown in Table 1. For one length-1 high-swu sequence, UL generates length-2 candidate sequences by joining it with other length-1 high-swu sequences which include it. For example, for length-1 candidate sequence $a$, length-2 candidate sequences $aa$, $ab$, $ac$, $ad$, $ae$, and $af$ are generated. As there are 6 length-1 candidate sequences, a total of $6 \times 6 = 36$ length-2 candidate sequences are generated, that is, for $N$ distinct items, $N^2$ length-2 sequences containing two elements will be generated. On the other hand, a length-1 candidate sequence joins with others to form length-2 single element candidate sequences, such as when sequence $a$ joins $b$, $c$, $d$, $e$, and $f$ to form $(ab)$, $(ac)$, $(ad)$, $(ae)$, and $(af)$. Similarly, sequence $b$ joins with $c$, $d$, $e$, and $f$ to form $(bc)$, $(bd)$, $(be)$, and $(bf)$. In this way, 5 candidate sequences for $a$, 4 candidate
sequences for $b$, 3 candidate sequences for $c$, 2 candidate sequences for $d$, and 1 candidate sequence for $e$ are generated. Accordingly, a total of $5+4+3+2+1=15$ ($(6\times5)/2$) candidate sequences are generated, that is, for $N$ distinct items, $(N^2(N-1))/2$ length-2 single-element candidate sequences will be generated. Hence, a total of $36+15=51$ length-2 candidate sequences are generated. The original SDB must be scanned once again with all these candidate sequences to detect the high-$swu$ sequences. It is noticeable that among the 51 candidates, 14 candidates, for example, $ca$, $cc$, $ef$, and $(ce)$, do not appear in the SDB at all. However, Table 1 also shows that 17 high-$swu$ sequences (candidate high-utility sequential patterns) are generated from these 51 candidates.

From level-3 to the last level, the UL algorithm generates high-$swu$ candidate sequences for $k$-th level by joining $L_{k-1}$ (high-$swu$ sequences for $(k-1)$-th level) with $L_k$. A sequence $X$ joins with another sequence $Y$ if the subsequence obtained by dropping the first item of $X$ is the same as the subsequence obtained by dropping the last item of $Y$. The new candidate sequence is formed by joining sequence $X$ with the last item of $Y$. The added item becomes a separate element if it was a separate element of $Y$, and otherwise, part of the last element of $X$. For example, length-2 high-$swu$ sequences $ab$ and $bd$ form length-3 candidate high-$swu$ sequence $abd$. On the other hand, length-2 high-$swu$ sequences $ab$ and $(bd)$ form length-3 candidate high-$swu$ sequence $abd$. After generating all the candidate high-$swu$ sequences by joining, UL algorithm prunes those candidate sequences having at least one subsequence which is not a length-$(k-1)$ high-$swu$ sequence. For example, after generating length-3 candidate high-$swu$ sequence $eae$ from length-2 high-$swu$ sequences $ee$ and $ae$, it prunes $eae$ as its subsequence $ee$ is not a high-$swu$ sequence. However, for level-3 of this example, this algorithm generates a total of 70 candidate sequences after joining and pruning and scans SDB again to detect 18 high-$swu$ sequences as shown in Table 1.

Similarly, it generates length-4 candidate high-$swu$ sequences and calculates 4 high-$swu$ sequences. No candidate high-$swu$ sequence is generated for level-5. Finally, it scans the SDB with these high-utility-$swu$ sequences to discover the high-utility sequential patterns. As a consequence, the UL algorithm discovers a total of 6 high-utility sequential patterns $<b$: 266, $(ab)$: 239, $(ab)d$: 238, $adbe$: 226, $(bd)ca$: 231, $(dab)e$: 250> by generating a total of 132 candidates and with five database scans.

2. US Algorithm

Even though our first proposed algorithm UL can discover the final resultant high-utility sequential patterns successfully, it suffers from the level-wise candidate generation-and-testing problem and hence generates a large number of candidate sequences. Moreover, its number of database scans is directly dependent on the maximum length of candidate sequences. Consider the example presented in the last section. It needs a total of 5 database scans as the maximum candidate length is 4 (last scan is needed for detecting high-utility sequential patterns from the high-$swu$ sequences). Hence, it needs a total of $N+1$ database scans for the maximum candidate length of $N$. Accordingly, it needs several database scans to find the resultant sequences.

To solve the problems of our first approach, in this subsection, we propose a second algorithm US. It exploits a
sequential pattern growth mining approach to avoid the level-
wise candidate generation-and-testing approach. Furthermore,
its number of database scan is independent on the maximum
candidate length. It always needs a maximum of three database
scans. Therefore, it significantly reduces the overall runtime for
mining high-utility sequential patterns.

First, the US algorithm scans the SDB once to detect
length-1 swu sequences. Subsequently, it generates projected
databases by considering length-1 swu sequences as prefixes
with a second database scan. Then, using a pattern growth
approach, it divides the search spaces (projected databases)
recursively and applies the same technique into them. By
utilizing this divide-and-conquer method, it generates very few
candidates compared to the UL algorithm. Note that the US
algorithm only generates the high-swu sequences without
generating a large number of intermediate candidate high-swu
sequences needed by the UL algorithm as shown in Table 2.

For prefix $a$, the UL algorithm generates a projected database
(shown in Table 2). Here, $(b)$ means that the last item in the
prefix, which is $a$, forms one element $(ab)$. However, in the
$a$-projected database, we get $<a: 310, b: 517, (ab): 602, d: 602,
e: 387, f: 130>$, and $c: 85>$. Items $c$ and $f$ cannot form a candidate
sequence with item $a$ as they have low-swu values (130 and 85,
respectively) in the $a$-projected database with respect to the
minSeqUtil. As a consequence, 6 candidate sequences $a: 602,
aa: 602, ab: 517, (ab): 602, ad: 602, and ae: 387$ are generated
here. Now, according to the divide-and-conquer rule, we apply
the same technique on the projected databases of $aa$, $ab$, $(ab),
ad$, and $ae$. The $aa$-projected database contains $<(_bd)fad: 130,
(_be): 180>$, and we get $<a: 130, (b): 310, d: 130, f: 130>$. Candidate sequences $aba: 310, a(b): 310, and a(b): 387$ are generated here. Similarly, the
other candidate sequences are generated. Table 2 shows that a
total of 17 candidate sequences are generated by prefix-$a$. It
also shows the other candidate sequences generated by other
prefix items. However, as mentioned earlier, the US algorithm
only generates the high-swu sequences as candidates. A third
database scan is needed to discover the high-utility sequential
patterns from the high-swu sequences. The US algorithm
discover the same set of resultant high-utility sequential
patterns $<b: 292, (ab): 239, (ab): 238, adbe: 226, a(bda): 231,
d(ab): 250>$. As discovered by the UL algorithm. However, in
this example, it generates only 45 candidates and scans the
database three times in contrast to the 132 candidates and five
data base scans of the UL algorithm.

3. Algorithm Description and Analysis

The UL algorithm first generates all the length-1 candidates for
high-swu sequences and calculates the set of length-1 high-swu
sequences (lines 1 and 2). Subsequently, it uses the for loop
described in lines 4 to 7 to determine the high-swu sequences for
other levels. In each level, it first generates the candidates (line 5)
and then scans the SDB for high-swu sequences (line 6). Finally,
it determines the high-utility sequential patterns from all the sets
of high-swu sequences (line 8).

The US algorithm first declares a set, $C$, and initializes to
NULL in order to contain all the high-swu sequences (lines 1
and 2). Then, it invokes the recursive US procedure (line 3).
This procedure is described in lines 4 to 14. Its three parameters
are described in line 5. At the beginning, it determines all the
high-swu items in the $a$-projected database $SDB_a$ (line 7).
Subsequently, it appends each high-swu item $β$ with $α$ in

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**Table 2. Candidate generation process for US algorithm.**

<table>
<thead>
<tr>
<th>Prefix</th>
<th>Projected SDB</th>
<th>Candidate high-utility seq. pattern (high-swu sequence) with swu values</th>
</tr>
</thead>
<tbody>
<tr>
<td>$c$</td>
<td>$(f)dbde: 74$</td>
<td>1 high-swu sequence $&lt;c: 226&gt;$</td>
</tr>
<tr>
<td>$f$</td>
<td>$ada: 130, b(de): 74, c: 67$</td>
<td>1 high-swu sequence $&lt;f: 271&gt;$</td>
</tr>
</tbody>
</table>
UL Algorithm.

Begin
Input: A sequence database SDB with utility values, minSeqUtil
Output: The complete set of high-utility sequential patterns
1. Let C1 be the set of length-1 candidates for high-swu sequences
2. Scan SDB once to find length-1 candidates
3. Let F1 be the set of length-1 high-swu sequences
4. for (k=2, Fk−1≠ NULL, k++)
5. Ck = generate length-k candidate swu sequences
6. Scan SDB once to find Fk
7. End for
8. Scan SDB once to find high-utility sequential patterns from UkFk
End

US Algorithm.

Begin
Input: An SDB with utility values, minSeqUtil
Output: The complete set of high-utility sequential patterns
1. Let C be the set of all high-swu sequences
2. Initialize C to NULL
3. Call US(NULL, 0, SDB)
4. Procedure US(α, len, SDB,)
5. Let α be a high-swu sequence, len is the length of α,
SDB is the α-projected sequence database if α+ NULL,
otherwise it is the SDB
6. Begin
7. Scan SDB once and find each high-swu item β, such that
(a) β can be appended to α to form a high-swu sequence
(b) β can be assembled to the last element of α to form
a high-swu sequence
8. For each high-swu item β
9. Append β with α in appropriate form to generate a
high-swu sequence α′
10. C = C U α′
11. Construct SDBβ
12. Call US(α′, len+1, SDBβ)
13. End For
14. End Procedure
15. Scan SDB once to discover all high-utility sequential patterns from C.
End

Therefore, it cannot appear as a candidate. Moreover, after determining X is a low-swu sequence, it is pruned. Accordingly, a candidate set of the US algorithm contains only the actual high-swu sequences; hence, N1 cannot be greater than N2.

V. Experimental Results

To evaluate the performance of our approach, we performed several experiments on synthetic datasets generated based on the principle introduced in [1] and using the source code available at [22]. These types of datasets have been used by most of the previous sequential data mining studies [1]-[5], [7], [19]-[21]. The parameters shown below are used to generate the datasets.

[D]: Number of customers
[C]: Average number of transactions per customer
[T]: Average number of items per transaction
[S]: Average length of maximal sequences
[L]: Average length of itemsets in maximal sequences
[N]: Number of distinct items

We generated two datasets for our experiments: D100K.C8.T6.S6.I5.N10K and D200K.C10.T8.S8.I7.N10K. Moreover, we used two real-life datasets: BMS-WebView-1 and BMS-WebView-2 [23], [24] contain web click-stream data. However, these datasets do not provide the internal and external utility values of the sequences. Most of the existing HUP mining algorithms [10]-[13] have generated random...
numbers for internal and external utilities. We have generated random numbers for internal and external utilities ranging from 1 to 10 and 1.0 to 10.0, respectively. Moreover, based on our observation in real-world databases that most items carry low profit, we generated the profit values using a log-normal distribution. Most of the HUP mining research [10]-[13] has adopted the same technique. Figure 2 shows the external utility distribution of 2,000 distinct items using a log-normal distribution. Our programs were written in Microsoft Visual C++ 6.0 and run with the Windows XP operating system on a Pentium dual core 2.13 GHz CPU with 2 GB main memory.

At first, we compared the performance of UL and US algorithms on the D100K.C8.T6.S6.I5.N10K dataset. Figure 3(a) shows the comparison with respect to number of candidate sequences. The minimum sequence utility threshold range of 0.1% to 0.9% was used here. The x-axis of Fig. 3(a) shows the different minimum sequence utility thresholds, and the y-axis shows the number of candidate sequences. As discussed in section IV, the UL algorithm generates a large number of candidates due to the level-wise candidate generation-and-testing methodology. On the other hand, the US algorithm generates fewer candidates compared to the UL algorithm by exploiting a pattern growth approach. The result of Fig. 3(a) reflects the analysis of section IV. Figure 3(b) shows the comparison with respect to runtime. The x-axis of Fig. 3(b) shows the different minimum sequence utility thresholds, and the y-axis shows the runtime. 

Subsequently, we compared the UL and US algorithms with respect to different SDB sizes on the D200K.C10.T8.S8.I7.N10K dataset as shown in Fig. 3(c). The x-axis of Fig. 3(c) shows the different number of sequences, and the y-axis shows the runtime. For each database size shown in the x-axis, two mining operations are performed with two different minimum sequence utility thresholds (2% and 5%) for each algorithm. Figure 3(c) shows that the US algorithm significantly outperforms the UL algorithm in all the stages in this dataset. It also demonstrates that the runtime increases when the number of sequences increases or the minimum sequence utility threshold decreases. Furthermore, it shows the scalability of our proposed algorithms with an increasing number of sequences in this SDB. The US algorithm is also memory-efficient compared to the UL algorithm since it generates a small number of candidates. The US algorithm needs

Finally, we compared our proposed algorithms with the existing algorithms. As discussed in section II, the existing approaches are based on the support measure. However, our framework is based on the utility measure. To show the significance and efficiency of our proposed two algorithms, we compared them with the SQUIRE approach. Even though it is based on the support measure, SQUIRE considers non-binary frequency values of items. Hence, it is more related to our approach than the other methods. Section II also mentions that the SQUIRE approach presents two Apriori-based algorithms, Apriori-QSP and Apriori-All, as well as two pattern growth-based algorithms, PrefixSpan-QSP and PrefixSpan-All. We compared our Apriori-based algorithm, UL, with the Apriori-QSP and Apriori-All algorithms. We compared our pattern growth-based algorithm, US, with the PrefixSpan-QSP and PrefixSpan-All algorithms.

We have used two real-life datasets BMS-WebView-1 and BMS-WebView-2 [23], [24] to compare our algorithms with the existing algorithms. These datasets contain several months’ worth of click-stream data from two e-commerce websites. Each transaction in these datasets is a web session consisting of all the product detail pages viewed in that session. That is, each product detail view is an item. The BMS-WebView-1 dataset has 59,602 transactions of 497 distinct items. The BMS-WebView-2 dataset has 77,512 transactions of 3,340 distinct items. The average transaction sizes are 2.5 and 5.0, respectively. In our experiments, an item is regarded as an item of a sequence, and a transaction is regarded as a sequence of items. Figure 4 shows the comparison of our Apriori-based algorithm UL with the existing Apriori-based algorithms, Apriori-QSP and Apriori-All, on the real-life BMS-WebView-1 dataset. Similarly, Fig. 5 shows the comparison of our pattern growth-based algorithm, US, with the pattern growth-based algorithms, PrefixSpan-QSP and PrefixSpan-All, on the real-life BMS-WebView-2 dataset.

The x-axes of Figs. 4 and 5 show the different number of sequences, and the y-axes shows the runtime. For each database size shown in the x-axes, a mining operation is performed with a minimum threshold of 0.06% in BMS-WebView-1 dataset (Fig. 4) and a minimum threshold of 0.05% in BMS-WebView-2 dataset (Fig. 5). For the existing algorithms, the minimum threshold value represents the minimum sequence utility value in a mining operation. Due to the support measure, the existing algorithms generate a large number of sequential patterns. In section II, it is noted that they are not applicable for high-utility sequential pattern mining. As a consequence, many unimportant sequential patterns may be generated with low-utility value. However, our algorithms use a utility measure and prune all the low-utility sequential patterns during the mining process. They avoid the generation of a huge amount of traditional sequential patterns and efficiently discover only high-utility sequential patterns. Therefore, our algorithms significantly outperform the existing algorithms as shown in Figs. 4 and 5.

Moreover, our algorithms also outperform the existing algorithms in memory usage since they avoid handling a large number of sequential patterns in the mining process. The UL algorithm needs 7.386 MB memory, the Apriori-All algorithm needs 12.109 MB memory, and the Apriori-QSP algorithm needs 15.724 MB memory on the BMS-WebView-1 dataset (minimum threshold=0.06%). The US algorithm needs 3.075 MB memory, the PrefixSpan-All algorithm needs 7.528 MB memory, and the PrefixSpan-QSP algorithm needs 10.491 MB memory on the BMS-WebView-2 dataset (minimum threshold=0.05%).
VI. Conclusion

In this paper, we proposed a novel framework for mining high-utility sequential patterns. Our proposed framework considers both internal and external utilities of a sequence and introduces a new measure, SeqUtility, to calculate the utility value of a sequence. It also defines the high-utility sequential patterns and the problem of mining high-utility sequential patterns. Furthermore, we proposed two new algorithms, UL and US, for mining high-utility sequential patterns. Of the two algorithms, UL is simpler and more straightforward for discovering high-utility sequential patterns. However, it suffers from the level-wise candidate generation-and-test problem and needs several database scans. The second algorithm, US, solves these problems by exploiting a sequential pattern growth approach. It generates a small number of candidates and needs a maximum of three database scans. Extensive performance analyses showed that our algorithms are very efficient and scalable for mining high-utility sequential patterns in sequence databases.

References

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