In Advanced Television Systems Committee (ATSC) terrestrial digital television (DTV) systems, additional very low-rate data can be transmitted by modulating the amplitude and polarity of the transmitter identification (TxID) signal. Although the additional data transmission scheme offers reliable transmission and has a very large coverage area, it has a limitation on the data rate. In this paper, we propose a novel additional data transmission scheme based on the TxID sequences of the ATSC DTV system and Walsh modulation. The proposed scheme not only increases the data rate significantly, but also offers a virtually identical coverage area compared to a conventional scheme.

Keywords: ATSC DTV, Kasami sequence, transmitter identification, Walsh sequence.
II. System Models

1. TxID Signal Transmission

The ATSC Standard A/110 introduces a particular form of pseudo-random noise sequences, referred to as Kasami sequences, to identify multiple transmitters and/or repeaters in SFNs [1]. The Kasami sequences are binary sequences of length $2^n-1$, where $n$ is an even integer. They comprise a large set, denoted as $K_L$, and a small set, denoted as $K_S$. Note that the large set includes all of the sequences in the small set. In addition, they have good auto-correlation and cross-correlation properties with large family sizes.

The Kasami sequence defined in the ATSC Standard A/110 is a large set with $n=16$, and the generator polynomial is given as $G(x) = G_1(x) \cdot G_2(x) \cdot G_3(x)$, where

$G_1(x) = x^{16} + x^{12} + x^8 + x^4 + 1$

$G_2(x) = x^{16} + x^{12} + x^9 + x^5 + x^4 + x^3 + x^2 + 1$

$G_3(x) = x^8 + x^7 + x^6 + x^5 + x^3 + x + 1$

As shown in Fig. 1, the Kasami sequence is modulated with two levels and scaled by a predetermined injection level before being added to the ATSC DTV signal. The total number of symbols in one field excluding a field sync segment is 259,584 (312 segments $\times$ 832 symbols/segment) [7], and the length of the Kasami sequence is 65,535 ($2^{16}-1$) [1]. As shown in Fig. 2, the ATSC Standard A/110 provides a scheme for embedding a Kasami sequence where the sequence of length 65,535 is repeated three times and the truncated sequence of length 62,979 is appended.

2. Conventional Scheme for Additional Data Transmission

To transmit additional data, each TxID sequence is modulated with input data. In [5], to transmit additional data using TxID signals, a polarity modulation was employed. Figures 3 and 4 show additional data transmission schemes of [5] with 40 bps and 160 bps, respectively. For the 40 bps mode, one polarity data bit is transmitted during one field duration. Note that the spreading factor of 40-bps mode is 259,584, and thus after dispreading, the SNR gain of $10\log_{10}259,584=54.1428$ dB is obtained. For 160-bps mode, on the other hand, one polarity data bit is transmitted during one (truncated) Kasami sequence, and thus 4 bits are transmitted during one field duration. Note that the spreading factor of 160-bps mode is 65,535 or 62,979. Hence, the spreading factor of 160-bps mode is decreased and the loss of the SNR gain is approximately 6 dB compared to the 40-bps mode.

In this manner, we can simply increase the data rate with a further reduced spreading factor. However, this straightforward scheme is very inefficient in the usage of the given bandwidth. Note that the simple decrease in the spreading factor inevitably induces the loss of the signal-to-noise ratio (SNR) gain and thus the noise margin of the system is severely degraded.

At the receiver, after multiplying the received signal by the reference Kasami sequence, the polarity is detected, and thus the transmitted data bits can be recovered from the resulting polarity [6].

Let us consider a single transmitter. The transmitted signal
can thus be written as
\[ s(n) = d(n) + \rho \sum_{j=1}^{4} v_j \{ P_j(n) x(n) \}, \]
where \( d(n) \), \( \rho \), and \( x(n) \) denote the DTV signal, injection level, and TxID sequence, respectively. Also, \( P_j(n) \) is given as
\[ P_j(n) = \begin{cases} 1, & (j-1)L_j + 1 \leq n \leq jL_j, \ j = 1, \ldots, 4, \\ 0, & \text{otherwise}, \end{cases} \]
and \( v_j \in \{-1, +1\} \), \( j = 1, \ldots, 4 \), denotes the polarity data corresponding to the \( j \)-th Kasami sequence where \( L_j \) denotes the length of the \( j \)-th Kasami sequence.

After passing through the channel \( h \), the received signal \( r(n) \) is given as
\[ r(n) = s(n) \ast h + w(n), \]
where \( w(n) \) is the noise at the receiver and \( \ast \) denotes the convolution operation.

To demodulate the polarity data \( v_j \), the received signal \( r(n) \) is correlated with the Kasami sequence \( x(n) \). The cross-correlation between \( r(n) \) and \( x(n) \) corresponding to the \( j \)-th Kasami sequence is then written as
\[ z_j = \sum_{n=L_j/(j-1)}^{n} r(n)x(n), \ j = 1, \ldots, 4. \]

By slicing \( z_j \), we can obtain the polarity data \( \hat{v}_j \) as
\[ \hat{v}_j = \text{sgn}\{z_j\}, \]
where \( \text{sgn}\{a\} \) denotes the sign of \( a \).

### III. Proposed Scheme for Additional Data Transmission

In this section, we propose a novel additional data transmission scheme for ATSC DTV systems. Figures 5 and 6 show the block diagram and principle of the proposed data transmission scheme, respectively. As shown in Fig. 5, first, \((1+\log_2M)\) data bits, \( b_0, b_1, \ldots, b_{k_6} \) are grouped and form a symbol using the serial-to-parallel converter, where \( M \) denotes the number of Walsh sequences used. The first bit, \( b_0 \), is the polarity data, and the group of the remaining \( M \) bits is one-to-one mapped to one of the \( M \) Walsh sequences of length \( M, w_1, w_2, \ldots, w_M \), where \( w_m = \{ w_{1_m}, w_{2_m}, \ldots, w_{M_m} \} \), \( w_{im} \in \{-1, +1\}, \ m = 1, 2, \ldots, M \), denotes the \( i \)-th Walsh sequence of length \( M \). The mapped Walsh sequence is then spread by the Kasami sequence of length \( L_k \) used for TxID. In other words, as shown in Fig. 6, each element \( w_{im} \) of the mapped Walsh sequence is sequentially spread by \( L/M \) chips of the Kasami sequence. The first \( L/M \) chips of the Kasami sequence are multiplied by the first element \( w_{1_1} \) of the Walsh sequence. In this manner, the last \( L/M \) chips of the Kasami sequence are multiplied by the last element \( w_{M_1} \) of the Walsh sequence. Finally, the resulting sequence is injected to the legacy ATSC DTV data with an appropriate injection level.

Again, let us consider the single transmitter case. The transmitted signal can then be written as
\[ s(n) = d(n) + \rho \sum_{j=1}^{M} \sum_{m=1}^{L/M} v_j \{ P_j(n) x(n) \} \{ c_{j,m} W_m(n) \}, \]
where
\[ W_m(n) = \begin{cases} 1, & (m - 1) \frac{L_j}{M} + 1 \leq n \leq m \frac{L_j}{M}, \ m = 1, \ldots, M, \\ 0, & \text{otherwise}, \end{cases} \]
and \( c_j = \{ c_{j,1}, \ldots, c_{j,M} \} \) denotes the Walsh sequence to be transmitted during the \( j \)-th Kasami sequence duration in a field where \( c_j \in \{ w_1, \ldots, w_M \} \). After passing through channel \( h \), the received signal \( r(n) \) is given by \( r(n) = s(n) \ast h + w(n) \).

At the receiver, the received signal is first multiplied by the reference Kasami sequence as
\[ z(n) = r(n) \cdot x(n) \]
\[ = \{ s(n) \ast h + w(n) \} \cdot x(n) \]
\[ = s(n) \ast h \cdot x(n) + w(n) \cdot x(n) \]
\[ = \rho \sum_{j=1}^{M} \sum_{m=1}^{L/M} v_j \{ P_j(n) x(n) \} \{ c_{j,m} W_m(n) \} \ast h \cdot x(n) \]
\[ = \rho v_j c_{j,m} \ast h + d(n) \ast h \cdot x(n) + w(n) \cdot x(n) \]
\[ = z_{j,m}(n), \]
where
\[ \begin{align*}
  z_{j,m}(n) &= \rho v_j c_{j,m} \otimes h + d(n) \otimes h \cdot x(n) + w(n) \cdot x(n), \\
  (j-1)L_j + \frac{m-1}{M}L_j &\leq n \leq (j-1)L_j + \frac{mL_j}{M}.
\end{align*} \tag{9}
\]

Recall that since the transmitted Walsh sequence is spread by the Kasami sequence of length \( L_j \) chips, each element of the Walsh sequence is spread by \( L_j/M \) chips of the Kasami sequence. Hence, as shown in Fig. 7, the received signal is despread by \( L_j/M \) chips of the Kasami sequence corresponding to each element of the Walsh sequence.

Let \( z_{jm}, m = 1, \ldots, M-1 \), denote the despread signal by \( L_j/M \) chips of the Kasami sequence corresponding to the \( m \)-th element of the Walsh sequence during \( j \)-th Kasami sequence duration. The despread signal, \( z_{jm}, j = 1, \ldots, 4, m = 1, \ldots, M \), can then be written as
\[
  z_{jm} = \sum_{n=(j-1)L_j}^{(j-1)L_j + \frac{m-1}{M}L_j} r(n) x(n)
  + \sum_{n=(j-1)L_j}^{(j-1)L_j + \frac{mL_j}{M}} z_{jm}(n)
  + \sum_{n=(j-1)L_j}^{(j-1)L_j + \frac{mL_j}{M} + 1} \left\{ \rho v_j c_{j,m} \otimes h \right\}
  + \sum_{n=(j-1)L_j}^{(j-1)L_j + \frac{mL_j}{M} + 1} \left\{ d(n) \otimes h \cdot x(n) + w(n) \cdot x(n) \right\}
  = \frac{L_j}{M} \rho v_j c_{j,m} \otimes h
  + \sum_{n=(j-1)L_j}^{(j-1)L_j + \frac{mL_j}{M} + 1} \left\{ d(n) \otimes h \cdot x(n) + w(n) \cdot x(n) \right\}. \tag{10}
\]

Now, the despread signal \( z_{jm}, m = 1, \ldots, M-1 \), is correlated with the Walsh sequences. The cross-correlation between \( \{z_{j,1}, \ldots, z_{j,4}\} \) and the Walsh sequence \( c_j = \{c_{j,1}, \ldots, c_{j,4}\} \) is given by
\[
  \begin{align*}
  \sum_{m=1}^{M} z_{j,m} c_{j,m} &= \sum_{m=1}^{M} \left\{ \frac{L_j}{M} \rho v_j c_{j,m} \otimes h \right\} \cdot c_{j,m} \\
  &+ \sum_{m=1}^{M} \left\{ (j-1)L_j + \frac{mL_j}{M} \right\} d(n) \otimes h \cdot x(n) \cdot c_{j,m} \\
  &+ \sum_{m=1}^{M} \left\{ (j-1)L_j + \frac{mL_j}{M} \right\} w(n) \cdot x(n) \cdot c_{j,m} \\
  &= L_j \rho v_j h \\
  &+ \sum_{m=1}^{M} \left\{ (j-1)L_j + \frac{mL_j}{M} \right\} \left\{ d(n) \otimes h \cdot x(n) \cdot c_{j,m} \right\} \\
  &+ \sum_{m=1}^{M} \left\{ (j-1)L_j + \frac{mL_j}{M} \right\} \left\{ w(n) \cdot x(n) \cdot c_{j,m} \right\}. \tag{11}
\end{align*}
\]

The Walsh sequence is detected by choosing the resulting correlation peak as
\[
  \hat{c}_j = \arg \max_{c_j} \left| \sum_{m=1}^{M} z_{j,m} c_{j,m} \right|. \tag{12}
\]

Note that \( \sum_{m=1}^{M} z_{j,m} c_{j,m} \) is the correlation between the Walsh sequence \( c_j \) and the despread signal \( z_{jm} \), and thus can efficiently be computed using the fast Walsh transform (FWT) [8]. An \( M \)-point FWT is applied to \( \{z_{j,1}, \ldots, z_{j,4}\} \), which gives \( \sum_{m=1}^{M} z_{j,m} c_{j,m} \) in (12). The computation of an \( M \)-point FWT requires \( M \log_2 M \) additions [8]. Hence, \( M^2 \log_2 M \) additions are required to compute (12).

Finally, we can obtain the polarity data \( \hat{v}_j \) by detecting the sign of the correlation peak for the detected Walsh sequence \( \hat{c}_j = \{\hat{c}_{j,1}, \ldots, \hat{c}_{j,M}\} \) as
\[
  \hat{v}_j = \text{sgn} \left( \sum_{m=1}^{M} z_{j,m} \hat{c}_{j,m} \right). \tag{13}
\]

Note that since four Walsh sequences are transmitted during one field, and the duration of one field is 24.2 ms, the achievable data rate\(^1\) of the proposed scheme is
\[
  \frac{4(1 + \log_2 M)}{24.2 \times 10^{-3}} \text{ (bps)}. \tag{14}
\]

\( 1 \) The maximum achievable data rate of the proposed scheme is 2.645 kbps (64 bits/24.2 ms) with \( M = 4^2 \).
IV. Performance Analysis

We assume that channel $h$ is constant during the transmission of at least one Kasami sequence. From (11), we can observe that the first term of the right side of (11) is the desired signal component, and the second term of the right side of (11) is the interference component due to the original DTV signal. Also, the third term of the right side of (11) is the noise component.

At the receiver, since the interference is despread by the Kasami sequence, we can assume that the interference component is modeled as Gaussian noise with variance $\sigma_w^2$. Then, at the output of the Walsh correlator, the SNR $\gamma$ can be written as

$$\gamma = 10\log_{10} \frac{L_j \rho \sigma_d^2}{\sigma_d^2 + \sigma_w^2},$$

(15)

where $\sigma_d^2$ denotes the received DTV signal power, and $\sigma_w^2$ denotes the noise variance.

Then, (15) can be rearranged as

$$\gamma = 10\log_{10} L_j + 10\log_{10} \rho \sigma_d^2 \sigma_w^2,$$

(16)

Note that the first term indicates the spreading gain by the Kasami sequence.

On the other hand, the carrier-to-noise ratio (CNR) can be written as

$$CNR = 10\log_{10} \frac{\sigma_d^2 + \rho \sigma_d^2}{\sigma_w^2} = 10\log_{10} \frac{\sigma_d^2}{\sigma_w^2} + 10\log_{10} (1 + \rho).$$

(17)

Then, from (16) and (17), $\gamma$ can be computed as

$$\gamma = 10\log_{10} L_j + CNR + 10\log_{10} \left(\frac{\rho}{1 + \rho + 10^{CNR/10}}\right).$$

(18)

As shown in (12) and (13), the detection rule of the proposed scheme can be interpreted as the detection rule of $M$-ary bi-orthogonal signaling. Therefore, we can obtain the symbol error rate (SER) of the proposed scheme as follows [9]:

$$P_s = 1 - \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} \left( \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} e^{-r^2/2} dx \right)^{M/2-1} e^{-r^2/2} dv.$$

(19)

Simulation results show that the interference component at the output of the Walsh correlator is well approximated as Gaussian noise and that the analytical form in (19) accurately predicts the SER of the proposed scheme.

V. Numerical Results

For all simulation results presented in this section, we assume that the injection level is $-30$ dB, that is, $\rho = 0.1449$. Figure 8 shows the average SER performance of the proposed scheme versus CNR under an additive white Gaussian noise (AWGN) channel. As shown in Fig. 8, the proposed scheme achieves a data rate of 2.314 kbps (56 bits/24.2 ms) with an SER of less than $10^{-3}$ under CNRs greater than 8 dB, which is approximately 11 times higher than the achievable data rate of [5] with 4-PAM. When the resulting sequence is injected 30 dB below the DTV signal, and $M$ is set to 64, the proposed scheme...
can achieve a data rate of 1.157 kbps (28 bits/24.2 ms) with an SER of less than $10^{-3}$ at CNRs greater than 1 dB, which is approximately 6 times higher than the achievable data rate of [5] with 4-PAM. Also, Fig. 8 shows that the analytical form (19) for the SER of the proposed scheme accurately predicts the simulation results.

Figure 9 shows the average bit error rate (BER) performance of the straightforward scheme with reduced spreading factors. We can observe that the performance of the straightforward scheme is severely degraded compared to the proposed scheme.

VI. Conclusion

In this paper, we proposed a novel data transmission scheme using TxID and Walsh sequences in ATSC DTV systems. The proposed scheme transmits data bits using a Walsh sequence and its polarity. The proposed scheme significantly enhances the data rate compared to the conventional schemes. The performance of the proposed scheme was theoretically analyzed. Also, the proposed scheme allows for an efficient receiver structure using an FWT.

References


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