Landing Dynamic and Key Parameter Estimations of a Landing Mechanism to Asteroid with Soft Surface

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Abstract
It is of great significance to utilize a landing mechanism to explore an asteroid. A landing mechanism named ALISE (Asteroid Landing and In Situ Exploring) for asteroid with soft surface is presented. The landing dynamic in the first turning stage, which represents the landing performance of the landing mechanism, is built by a Lagrange equation. Three key parameters can be found influencing the landing performance: the retro-rocket thrust $T$, damping element damping $c_1$, and cardan element damping $c_2$. In this paper, the retro-rocket thrust $T$ is solved with considering that the landing mechanism has no overturning in extreme landing conditions. The damping element damping $c_1$ is solved by a simplified dynamic model. After solving the parameters $T$ and $c_1$, the cardan element damping $c_2$ is calculated using the landing dynamic model, which is built by Lagrange equation. The validities of these three key parameters are tested by simulation. The results show a stable landing, when landing with the three estimated parameters $T$, $c_1$, and $c_2$. Therefore, the landing dynamic model and methods to estimate key parameters are reasonable, and are useful for guiding the design of the landing mechanism.

Key words: asteroid landing mechanism, landing dynamic, landing performance, damping

1. Introduction
There are enormous asteroids formed at the beginning of the solar system. Most of them are rich in minerals, and some of them are dangerous to the Earth [1, 2]. Thus, exploring the asteroids is of great significance, with the purpose of obtaining great economic effectiveness, and protecting the Earth. Landing on an asteroid is a great step towards exploring these asteroids, and its merits include: 1) learning about asteroids in situ; 2) changing dangerous asteroid orbits; 3) using asteroids as platforms to observe other celestial bodies; 4) using asteroids as carrying devices; 5) establishing communication stations on asteroids, and 6) capturing asteroids with minerals and bringing them back to earth [3, 4]. However, these merits can only be carried out after a lander is able to land safely on an asteroid. Landing safely or not is represented by the landing performance, and the landing performance is usually evaluated by both the overloading acceleration and stability time, which are included in the landing dynamic model. Thus, it is of great significance to estimate the key parameters that will induce a good landing performance, by building a landing dynamic model. Besides, the values of these key parameters can guide the design of the landing mechanism.

Presently, most of the landing dynamic models are designed for lunar landing mechanisms, but are not suited to small body landing mechanisms, because of different landing environments, with different landing strategies [5-11]. The Europe Space Agency (ESA), National Aeronautics and Space Administration (NASA), and Japan Aerospace Exploration Agency (JAXA) have developed small body landing mechanisms, but the landing dynamic model is rarely used to evaluate the landing performance, and to guide the design of the landing mechanism [12-16]. They just evaluate the landing performance by simulation with the given value of the parameters, but don’t show how these values are educed [17].

In this paper, an Asteroid Landing and In Situ Exploring (“ALISE”) landing mechanism for asteroid with soft surface...
is presented. The landing dynamic model in the first turning stage is built by Lagrange equation. It can be found that there are three key parameters (retro-rocket thrust $T$, damping element damping $c_1$, and cardan element damping $c_2$) that will influence the landing performance. Thus, the values of these three parameters must be estimated, to achieve excellent landing performance. The paper firstly estimates the value of $T$, by considering that the retro-rocket will prevent the landing mechanism from overturning, by counteracting the turning energy. Secondly, the value of $c_1$ is estimated by a simplified dynamic model. Thirdly, after defining the values of $T$ and $c_1$, the value of $c_2$ is calculated by the landing dynamic model, with the objective function of having the shortest stability time, and the constraint condition that the overloading acceleration is less than 10g. Lastly, the validities of these three values are tested, by simulating the landing performance in Adams software.

2. The ALISE landing mechanism

The ALISE landing mechanism aims at asteroids with soft surface (especially C type asteroid), which are softer than other asteroids, because of containing organic materials and amino acids [18, 19], and the design is inspired by the Rosetta lander and the ST4/Champollion lander [20-22]. The ALISE landing mechanism includes a three-leg landing gear, and an anchoring system that is designed to avoid the flying away of the lander under low gravity. The landing gear contains landing foot, landing legs, cardan element, damping element, and equipment base. The damping element is realized by electromagnetic damping, which is a new technology in deep space exploration. This damping mode has the merits of high efficiency, easy control, adjustable damping, and so on, and has been used in the Rosetta landing mechanism [20]. The anchoring system contains anchoring element, propulsion element, rewinding element, and cushion element. The schematics and performance parameters are shown separately in Fig. 1 and Table 1. Besides, the retro-rocket is fixed on the upper surface of the equipment base, to supply thrust towards the landing slope, to prevent the rebound of the landing mechanism, when landing. There is no sign of the retro-rocket in the schematics, because it is a part of the control system, but not a part of the mechanical structure.

There are awls beneath the landing feet to prevent sliding, and contact switches inside the landing feet, to generate landing signals. The cardan element has the functions of both absorbing the horizontal impact when landing, and adjusting the attitude of the equipment base after landing, while the damping element is just used to absorb the vertical impact. The anchoring element, which connects to the rewinding element via a thread, will be pushed rapidly into the asteroid by the propulsion element. At the time of penetration of the anchoring element, the rewinding element will quickly rewind the thread. When the thread is instantaneously tense, the cushion element, which is composed of a compression spring, will absorb the impact, to protect the rewinding motor. The retro-rocket will be activated at the time of landing, and supply a constant force lasting about 5 seconds toward the equipment base, to prevent the landing mechanism from rebounding.

3. Landing dynamic model

The surface of the asteroid with soft surface is soft. When landing, the awls will penetrate the asteroid some depth, to prevent sliding of the landing mechanism, and the retro-rocket would be activated, to counteract the rebound of the

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Table 1. Mechanical and landing performance parameters

<table>
<thead>
<tr>
<th>Items</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Landing gear mass</td>
<td>45 kg</td>
</tr>
<tr>
<td>Payload mass</td>
<td>≤ 55 kg</td>
</tr>
<tr>
<td>Anchoring system mass</td>
<td>1 kg</td>
</tr>
<tr>
<td>Horizontal velocity</td>
<td>≤ 0.5 m/s</td>
</tr>
<tr>
<td>Vertical velocity</td>
<td>≤ 1.5 m/s</td>
</tr>
<tr>
<td>Landing slope</td>
<td>≤ 30°</td>
</tr>
<tr>
<td>Medium tensile strength</td>
<td>0.5 MPa ≤ $T_1$ ≤ 5 MPa</td>
</tr>
<tr>
<td>Anchoring time</td>
<td>≤ 5 s</td>
</tr>
<tr>
<td>Anchoring force</td>
<td>≥ 100 N</td>
</tr>
<tr>
<td>Penetration velocity</td>
<td>50 m/s–100 m/s</td>
</tr>
<tr>
<td>Rewinding force</td>
<td>About 20 N</td>
</tr>
<tr>
<td>Thread length</td>
<td>2 m</td>
</tr>
</tbody>
</table>

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Fig. 1. Schematic of the landing mechanism
landing mechanism. Then, the landing mechanism will turn clockwise or counterclockwise around the feet’s anchoring points. The interaction between the avs and the surface is three-dimensional and very complicated, and few reasonable models can express this interaction accurately. Furthermore, the dynamic parameters in the first turning stage are enough to express the landing performance. Thus, the paper only develops the landing dynamic of the first turning stage. There are two-dimensional and three-dimensional landing dynamic models. But considering that the two-dimensional model is successfully adopted by the lunar lander, and that it is simpler than the three-dimensional model, a two-dimensional landing dynamic is built for the ALISE landing mechanism.

Some hypotheses are made in building the landing dynamic model: 1) the gravity on the asteroid is of the order of magnitude about 10^-4 m/s^2, therefore the gravity is ignored; 2) the friction between the landing feet and landing legs is ignored; 3) The stiffness of the landing gear is far greater than that of the damping element vertically, and of the cardan element horizontally. So the flexibility of the landing gear is ignored; 4) the impulse acting on the landing mechanism when shooting the anchoring system is ignored; 5) the overturning of the landing mechanism is over, before the anchoring system tenses the thread.

As shown in the right part of Fig. 2, the landing mechanism will turn around the point O when landing. The whole system has three degrees of freedom: rotational DOF of m1; translational DOF of m2; and translational DOF of m1. The Lagrange equation is introduced, to build the landing dynamic model. The kinetic energy \( T \), potential energy \( V \), and Rayleigh’s Dissipation Function \( \psi \) are shown in equations (1) and (2) respectively. The meanings and values of the parameters in equations (1) and (2) are shown in Table 2.

\[
\begin{align*}
T &= \frac{1}{2} J_{\text{sc}} \dot{\phi}^2 \quad \text{and} \quad \frac{1}{2} m_1 \dot{\phi}_1^2 \quad \text{and} \quad \frac{1}{2} m_1 \dot{\phi}^2 + m_1 \dot{\phi}_1 \dot{\phi} + m_1 g \left[ \sin(\phi_1 - \phi) + \sin(\phi - \phi_1) \right]
\end{align*}
\]

\[
\psi = \frac{1}{2} c_1 \dot{s}^2 + \frac{1}{2} c_2 (\dot{\phi}_1 - \dot{\phi})^2
\]

Then, the Lagrange dynamic equations are deduced, as shown in equations (3), (4) and (5).

\[
\begin{align*}
\tau_1 &= m_1 \ddot{x} = m_1 \ddot{\phi}_1 \left[ \sin(\phi_1 - \phi) - \sin(\phi - \phi_1) \right] - m_1 g \cos(\phi_1 - \phi)
\end{align*}
\]

\[
\begin{align*}
\tau_2 &= m_1 \ddot{y} = m_1 \ddot{\phi}_1 \left[ \cos(\phi_1 - \phi) - \cos(\phi - \phi_1) \right]
\end{align*}
\]

\[
\begin{align*}
0 &= J_{ss} \ddot{\phi} + m_2 \ddot{s} \quad \text{and} \quad m_2 \ddot{\phi}_2 \quad \text{and} \quad m_2 \ddot{\phi}_1 - m_1 \ddot{s} \quad \text{and} \quad m_1 \ddot{\phi}_1 - m_2 \ddot{s}
\end{align*}
\]

The parameters \( s, \phi_1, \phi_2, \dot{s}, \dot{\phi}_1, \dot{\phi}_2 \) of landing dynamic characteristics can be solved by equations (3), (4) and (5) with the initial values. However, in a complicated landing impact, the initial values are difficult, or impossible to solve accurately - they can only be estimated. A schematic of the impact is shown in the left part of Fig. 2. Firstly, the impacting force acting on m1 at point O is far larger than the other external force, thus the impulse of m2 acting on m1 can be ignored. So the angular momentum of m1 around O is conservational. Secondly, ignoring the retro-rocket thrust \( T \), the angular momentum of the system composed of m1 and m2 is conservational. Thirdly, there is a damping element between the m1 and m2 vertically, therefore the vertical velocity of the m2 changes continuously. Therefore the following equation (6) can be deduced. Meanings and values of the parameters in equation (6) are shown in Table 2.

\[
\begin{align*}
0 &= \left[ 1 J_1 + m_2 a \right] \omega_1 - \left[ m_2 h - m_2 \dot{h} \right] \\
0 &= \left[ 1 J_2 + m_2 a \right] \omega_2 + \left[ m_2 h + m_2 \dot{h} \right] b_2 - \left[ m_2 h - m_2 \dot{h} \right] a \dot{\omega}_2 V_{2y}
\end{align*}
\]

where, \( \omega_1, \omega_2 \) and \( V_{2y} \) can be calculated from equations (6). Thus, the initial values to solve the equations (3), (4) and (5) are obtained, as shown in equation (7).
\[s(t=0)=S_1\]
\[\phi_1(t=0)=0\]
\[\phi_2(t=0)=0\]
\[\dot{s}(t=0)=V_{21y}\]
\[\dot{\phi}_1(t=0)=\omega_1\]
\[\dot{\phi}_2(t=0)=\omega_2\]

(7)

4. Estimations of the key parameters T, \(c_1\) and \(c_2\)

From the landing dynamic model, as shown in equations (3), (4) and (5), it can be found that the landing performance parameters \(s\), \(\phi_1\), \(\phi_2\), \(\delta\), \(\phi_1\), \(\delta\), \(\phi_2\) are determined by \(T\), \(c_1\) and \(c_2\). So to have a superior landing performance, it is necessary to determine the proper values of \(T\), \(c_1\), and \(c_2\).

4.1 Estimation of retro-rocket thrust \(T\)

The retro-rocket supplies constant force \(T\) towards the upper surface of the equipment base, to prevent the landing mechanism from rebounding and overturning. In order to find the safe thrust, it is assumed that the landing mechanism is a rigid body, and its initial kinetic energy is counteracted entirely by the retro-rocket thrust. There are counterclockwise overturning, and clockwise overturning. They need different values of thrust, to prevent overturning. Thus, it is necessary to estimate the thrust separately for the two types of overturning, and then the largest value is taken as the retro-rocket thrust value.

4.1.1 Counterclockwise overturning

When landing with the initial velocity \(V_1=0.5\) m/s and \(V_1=0\) m/s in 2-1 mode, the landing mechanism will turn counterclockwise, and have the most possibility to overturn counterclockwise. This schematic is shown in the left part of the Fig. 3. The meanings and values of the parameters in the schematic are shown in Table 3.

The landing mechanism turns around the O point counterclockwise after impact, and the initial overturn angular velocity \(\omega_1\) can be estimated from the angular momentum conservation of \(m\) around O. Thus, the following equation is obtained:

\[-m^2b\left[1+ma(x^2+y^2)\right]\omega_1\]

(8)

The solution of equation (8) is:

Table 2.2 Meanings and values of the parameters

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Meaning</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>mass beneath cardan element</td>
<td>22kg</td>
</tr>
<tr>
<td>m_1</td>
<td>mass above cardan element</td>
<td>78kg</td>
</tr>
<tr>
<td>m_2</td>
<td>inertia</td>
<td>3.54kg m^2</td>
</tr>
<tr>
<td>J_1</td>
<td>m_1 inertia</td>
<td>4.79kg m^2</td>
</tr>
<tr>
<td>J_2</td>
<td>m_2 inertia</td>
<td></td>
</tr>
<tr>
<td>L_1</td>
<td>length between m_1 and O</td>
<td>1.001m</td>
</tr>
<tr>
<td>S_1</td>
<td>length between m_1 and c_2</td>
<td>0.163m</td>
</tr>
<tr>
<td>S_2</td>
<td>initial length from m_1 to c_2</td>
<td>0.344m</td>
</tr>
<tr>
<td>a</td>
<td>m_1 abscissa length</td>
<td>0.927m</td>
</tr>
<tr>
<td>b_1</td>
<td>m_1 ordinate length</td>
<td>0.388m</td>
</tr>
<tr>
<td>b_2</td>
<td>m_2 ordinate length</td>
<td>0.895m</td>
</tr>
<tr>
<td>\alpha</td>
<td>initial angle between y axis and Om_1</td>
<td>67.3°</td>
</tr>
<tr>
<td>\theta</td>
<td>landing slope angle</td>
<td>0~30°</td>
</tr>
<tr>
<td>V_1</td>
<td>horizontal landing velocity</td>
<td>-0.5~0.5 (m/s)</td>
</tr>
<tr>
<td>V_2</td>
<td>vertical landing velocity</td>
<td>-1.5~0 (m/s)</td>
</tr>
<tr>
<td>T</td>
<td>retro-rocket thrust</td>
<td>variable</td>
</tr>
<tr>
<td>c_1</td>
<td>damping element damping</td>
<td>variable</td>
</tr>
<tr>
<td>c_2</td>
<td>cardan element damping</td>
<td>variable</td>
</tr>
<tr>
<td>s</td>
<td>m_2 translation relative to m_1</td>
<td>related to (c_1, c_2, T)</td>
</tr>
<tr>
<td>\phi_1</td>
<td>m_1 rotation angle</td>
<td>related to (c_1, c_2, T)</td>
</tr>
<tr>
<td>\phi_2</td>
<td>m_2 rotation angle</td>
<td>related to (c_1, c_2, T)</td>
</tr>
<tr>
<td>\alpha_1</td>
<td>initial angular velocity</td>
<td>related to (V_x, V_y)</td>
</tr>
<tr>
<td>\alpha_2</td>
<td>m_2 initial angular velocity</td>
<td>related to (V_x, V_y)</td>
</tr>
<tr>
<td>V_{21y}</td>
<td>m_2 initial vertical velocity relative to m_1</td>
<td>related to (V_x, V_y)</td>
</tr>
</tbody>
</table>
\[ \omega_2 = \frac{-mV_y b}{J_m + m(a^2 + b^2)} = 0.41 \text{ rad/s} \] (9)

The largest allowable turning range of the landing mechanism without overturning is from \( P_1 \) to \( P_2 \). So the initial kinetic energy of the landing mechanism after impact should be counteracted totally by the retro-rocket thrust \( T_1 \) during the angle \( \angle P_1OP_2 \), which equals \( \pi/2 \). Therefore, the following equation is obtained:

\[ \frac{1}{2} \left[ J_1 + m(a^2 + b^2) \right] \omega_{1i}^2 = T_1 \omega_{1i} \frac{\pi}{2} \] (10)

Obtaining:

\[ T_1 = \frac{1}{\pi \omega_{1i}^2} \left[ J_1 + m(a^2 + b^2) \right] = 11.04 \text{ N} \] (11)

where, \( T_1 \) is the retro-rocket thrust preventing the landing mechanism from counterclockwise overturning.

4.1.2 Clockwise overturning

When landing with the initial velocity \( V_x=0.5 \text{m/s} \) and \( V_y=1.5 \text{m/s} \) in 1-2 mode, the landing mechanism will turn clockwise, and have the most possibility to overturn clockwise. This schematic is shown in the right part of Fig. 3. The meanings and values of the parameters in the schematic are shown in Table 2 and Table 3.

The landing mechanism turns around the \( O \) point clockwise after impact, and the initial turning angular velocity \( \omega_{1i} \) can be estimated from the angular momentum conservation of \( m \) around \( O \). Thus, the following equation is obtained:

\[ mV_y b - mV_x a = \left( J_1 + m(a^2 + b^2) \right) \omega_{1i} \] (12)

Obtaining:

\[ \omega_{1i} = \frac{mV_y b - mV_x a}{J_1 + m(a^2 + b^2)} = 1.11 \text{ rad/s} \] (13)

When the landing mechanism turns to the \( P_1 \) position with the retro-rocket thrust \( T_2 \), the angular velocity \( \omega_{2i} \) can be calculated by the energy conversion.

\[ \omega_{2i} = \sqrt{\frac{1}{J_m + m(a^2 + b^2)} \left[ J_1 + m(a^2 + b^2) \right] \omega_{1i}^2 + 2T_2 a \theta} \] (14)

The tangential velocity of \( m \) in the \( P_2 \) position is:

\[ V_{2i} = \omega_{2i} \sqrt{a^2 + b^2} \] (15)

Then the landing mechanism will turn continuously around point \( B \). It is assumed that the recovery coefficient \( e \) equals 0.6 between the landing mechanism and the landing surface (\( e \) equals 0.5 between wood and wood; \( e \) equals 0.56 between steel and steel). Thus, the rebound velocity \( V_{2i} \) can be expressed as:

\[ V_{2i} = eV_{1i} \cos \beta \] (16)

Then the initial angular velocity \( \omega_{2i} \) around the point \( B \) is obtained:

\[ \omega_{2i} = \frac{V_{2i}}{P_2 B} = \frac{V_{2i}}{\sqrt{a^2 + b^2}} \] (17)

The largest allowable turning range of the landing mechanism, without overturning, is from \( P_2 \) to \( P_3 \). So the kinetic energy of the landing mechanism after \( P_2 \) position should be counteracted totally by the retro-rocket \( T_2 \) during the angle \( \angle P_3BP_2 \), which equals \( \pi/2 - \theta \). Thus, the following equation is obtained:

\[ \frac{1}{2} \left[ J_1 + m(a^2 + b^2) \right] \omega_{2i}^2 = T_2 \omega_{2i} \left( \frac{\pi}{2} - \theta \right) \] (18)

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Meaning</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( m )</td>
<td>total mass of ( (m_1 + m_2) )</td>
<td>100kg</td>
</tr>
<tr>
<td>( J_1 )</td>
<td>inertia of ( (m_1 + m_2) )</td>
<td>12.7kg·m²</td>
</tr>
<tr>
<td>( a' )</td>
<td>m abscissa length</td>
<td>0.4635m</td>
</tr>
<tr>
<td>( b )</td>
<td>m ordinate length</td>
<td>0.784m</td>
</tr>
<tr>
<td>( \theta )</td>
<td>landing slope angle</td>
<td>30°</td>
</tr>
<tr>
<td>( \beta )</td>
<td>mechanical determined</td>
<td>38°</td>
</tr>
</tbody>
</table>

Table 3. Meanings and values of the parameters

Fig. 3. Turning schematics of the landing mechanism
Combining equations (13-18) yields the retro-rocket thrust $T_2$:

$$T_2 = \frac{5194.5e^2}{38.8 - 25.57e^2}$$

(19)

Substituting $e$ with 0.6, we obtain:

$$T_2 = 63.2 \text{N}$$

(20)

The final retro-rocket thrust $T$ should be no less than $T_1$ or $T_2$. In the paper, the retro-rocket thrust $T$ is set to 65 N.

4.2 Estimation of the damping element damping $c_1$

The dynamic model of the landing mechanism in the vertical direction could be simply expressed as Fig. 4 and equation (21), in which $k$ is the stiffness of the landing mechanism.

$$\begin{align*}
&m_1 \ddot{x}_1 - c_1 (x_1 - \dot{x}_1) + kx_1 = 0 \\
&m_2 \ddot{x}_2 + c_1 (x_1 - \dot{x}_1) = 0
\end{align*}$$

(21)

The initial conditions of equation (21) can be written as follows:

$$\begin{align*}
&x_1 (t = 0) = 0 \\
&\dot{x}_1 (t = 0) = V_{x1} = 1.5 \\
&x_2 (t = 0) = 0 \\
&\dot{x}_2 (t = 0) = V_{x2} = 1.5
\end{align*}$$

(22)

The overloading accelerations of $m_2$ are different, on account of different $c_i$. When the damping $c_i$ equals 900 Ns/m, the numerical solution of the equation (21) is shown in Fig. 5. It can be found that the overloading acceleration of $m_2$ is 30 m/s$^2$, and the stroke of the damping is 0.13 m. These overloading acceleration and stroke are feasible for the landing mechanism. Thus, the parameters of the damping element are set to $c_i = 900$ Ns/m and $S = 0.13$ m, respectively.

4.3 Calculation of cardan element damping $c_2$

The $c_2$ is a rotational damping produced by two motors in the cardan element, and it is used to absorb the horizontal impact when landing. Therefore, the value of $c_2$ can be changed, by controlling the motors. The landing performance in changing $c_2$ that is varied depending on different initial landing velocities, will be better compared with that in constant $c_2$.

The value of $c_2$ can be calculated through the landing dynamic model shown in equations (3), (4), (5) with proper objective function and constraint conditions, after determining the values of $T$ and $c_1$.

In the landing dynamic model, it can be found that during the turning, $c_2$ will influence the angular momentum of $m_2$. The smaller the angular momentum of $m_2$, the harder the landing mechanism is to overturn. Thus, the smaller angular momentum of $m_2$ is to be the objective function to solve $c_2$. The constraint conditions to solve $c_2$ are: 1) the horizontal overloading acceleration of $m_2$ is less than 10 g; 2) the turning angle of $m_2$ relative to $m_1$ is less than $10^\circ$. The flow chart to calculate $c_2$ is shown in Fig. 6.

The values of $c_2$ solved with different landing velocities are shown in Fig. 7. The data in Fig. 7 can be expressed as counter in Fig. 8. The landing mechanism will have a more stable landing when $c_2$ varies with $V_i$ and $V_j$ according to the...
relationship shown in Fig. 7 or Fig. 8. The varying range of \( c \) is between 17 Nm/s/rad and 111 Nm/s/rad.

5. Landing simulation

The validities of the landing dynamic model and the parameters \( T, c_1, c_2 \) need to be verified, by testing the landing performance. In the paper, the famous Adams software is used to simulate the landing performance. The landing mechanism has three classic landing modes, called 1-2 mode, 2-1 mode and 1-1-1 mode, respectively. Thus, the landing performances are tested in these three landing modes. The simulation parameters are shown in Table 4.

5.1 Verification of the key parameters

The landing performances in extreme landing conditions \((V_y = -0.5 \text{ m/s, } V_y = -1.5 \text{ m/s})\) are tested with the estimated parameters \( T, c_1, c_2 \). The overloading acceleration of the equipment base reflects the damping performance, and the angular velocity of the landing legs reflects the stability time. Their values in the three classic landing modes are shown in Fig. 9. The left graph shows that the largest overloading accelerations of the equipment base are: about 80 m/s\(^2\) in 1-2 mode; about 30 m/s\(^2\) in 2-1 mode, and about 90 m/s\(^2\) in 1-1-1 mode. The right graph shows that the stability times are: about 3.6 second in 1-2 mode; about 1.5 second in 2-1 mode and about 3.7 second in 1-1-1 mode. It can be found that the overloading accelerations are all less than 10g, and the landing stability times are all less than 4 second. Thus, the estimations of the parameters \( T, c_1 \) and \( c_2 \) are valid.

5.2 Influence of \( c_2 \) on the landing performance

There are two modes of \( c_2 \) to select when landing: one is constant \( c_2 \) \((c_2 \) remains constant at about 111 Nms/rad\) in all

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lander mass (lower)</td>
<td>22 kg</td>
</tr>
<tr>
<td>Lander mass (upper)</td>
<td>78 kg</td>
</tr>
<tr>
<td>Vertical velocity ( V_y )</td>
<td>0–1.5 m/s</td>
</tr>
<tr>
<td>Horizontal velocity ( V_x )</td>
<td>-0.5–0.5 m/s</td>
</tr>
<tr>
<td>Damping element damping</td>
<td>900 N/m</td>
</tr>
<tr>
<td>Cardan element damping</td>
<td>17–111 (Nms/rad)</td>
</tr>
<tr>
<td>Retro-rocket thrust</td>
<td>65 N</td>
</tr>
<tr>
<td>Friction coefficient</td>
<td>2.0</td>
</tr>
<tr>
<td>Landing slope stiffness</td>
<td>50000 N/m</td>
</tr>
<tr>
<td>Asteroid gravity</td>
<td>0 g</td>
</tr>
<tr>
<td>Landing mode</td>
<td>1-2, 2-1, 1-1-1</td>
</tr>
<tr>
<td>Landing slope angle</td>
<td>30°</td>
</tr>
</tbody>
</table>

Notes: Lines “mag_acc” represent the respective overloading accelerations of the equipment base. Lines “mag_ang_vel” represent the respective angular velocities of the landing legs.
landing velocities), the other is optimal \( c_2 \) (\( c_2 \) varies according to different initial landing velocities, as the rules shown in Fig. 7 or Fig. 8). Constant \( c_1 \) has the merits of easy control, whereas optimal \( c_2 \) can induce a better landing performance. The landing performances between the two modes of \( c_2 \) are compared in three classic landing modes, in the conditions that \( V_x = 0.1 \) m/s and \( V_y = -0.5 \) m/s, respectively. The optimal \( c_2 \) in relation to \( V_x = 0.1 \) m/s and \( V_y = -0.5 \) m/s is 55 Nms/rad, which is shown in Fig. 7 and Fig. 8. The landing performance simulation results are shown in Fig. 10, Fig. 11 and Fig. 12, respectively, and the maximum overloading accelerations and stability times shown in these figures are summarized in Table 5. It can be found that both the maximum overloading accelerations and stability times with constant \( c_2 \) are all larger, than that with optimal \( c_2 \). Thus, optimal \( c_2 \) would lead to better landing performance.

![Fig. 10. Landing performance in 1-2 mode with different cardan element damping \( c_2 \)](image)

Notes: Real lines “1-2 con_mag_acc” and “1-2 con_mag_ang_vel” represent the overloading acceleration of the equipment base, and angular velocity of the landing legs, respectively, with constant \( c_2 \) in 1-2 landing mode. Dashed lines “1-2 var_mag_acc” and “1-2 var_mag_ang_vel” represent the overloading acceleration of the equipment base, and angular velocity of the landing legs, respectively, with optimal \( c_2 \) in 1-2 landing mode.

![Fig. 11. Landing performance in 2-1 mode with different cardan element damping \( c_2 \)](image)

Notes: Real lines “2-1 con_mag_acc” and “2-1 con_mag_ang_vel” represent the overloading acceleration of the equipment base, and angular velocity of the landing legs, respectively, with constant \( c_2 \) in 2-1 landing mode. Dashed lines “2-1 var_mag_acc” and “2-1 var_mag_ang_vel” represent the overloading acceleration of the equipment base, and angular velocity of the landing legs, respectively, with optimal \( c_2 \) in 2-1 landing mode.

![Fig. 12. Landing performance in 1-1-1 mode with different cardan element damping \( c_2 \)](image)

Notes: Real lines “1-1-1 con_mag_acc” and “1-1-1 con_mag_ang” represent the overloading acceleration of the equipment base, and angular velocity of the landing legs, respectively, with constant \( c_2 \) in 1-1-1 landing mode. Dashed lines “1-1-1 var_mag_acc” and “1-1-1 var_mag_ang” represent the overloading acceleration of the equipment base, and angular velocity of the landing legs, respectively, with optimal \( c_2 \) in 1-1-1 landing mode.
6. Conclusions

A landing mechanism for asteroid with soft surface is presented. Reasonable values of the three key parameters (retro-rocket thrust $T$, damping element damping $c_1$, and cardan element damping $c_2$) that influence the landing performance of the landing mechanism presented in the paper are: $T=65N$; $c_1=900Ns/m$; and $c_2$ changes between 17 Nms/rad and 111Nms/rad, in relation to the initial landing velocities. The overloading accelerations of the equipment base are less than 10g, and the stability times are less than 5s, when landing with the estimated values of $T$, $c_1$, and $c_2$. Furthermore, optimal $c_2$ in relation to the landing velocities will lead to a good landing performance, with comparison to constant $c_2$. The simulation results show that the landing dynamic model, and the methods to estimate key parameters, are reasonable. The estimations of key parameters can be used to guide the design of the landing mechanism.

In future, the landing mechanism will be manufactured, and then the validities of the landing mechanism and its parameters will be tested physically, under microgravity.

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References


| Table 5. Landing performances with constant and optimal $c_2$ in three landing modes |
|---------------------------------|---------------|---------------|---------------|
|                                | 1-2 landing mode | 2-1 landing mode | 1-1-1 landing mode |
| Maximum overloading acceleration | Constant $c_2$ | 90 m/s² | 38 m/s² | 52 m/s² |
|                                | Optimal $c_2$ | 18 m/s² | 30 m/s² | 48 m/s² |
| Stability time                 | Constant $c_2$ | 2.8 s | 1.5 s | 2.8 s |
|                                | Optimal $c_2$ | 2.6 s | 1.0 s | 2.6 s |
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