Distribution of Organic Matter and Al_{0}+1/2Fe_{0} Contents in Soils Using Principal Component and Multiple Regression Analysis in Jeju Island

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The contents of soil organic matter (SOM) and Al_{0}+1/2Fe_{0} in soils are important criteria for the classification of new Andisols in Soil Taxonomy system. There are many soil types in Jeju Island with various soil forming environments. This paper was conducted to estimate the contents of soil organic matter and the content of ammonium oxalate extracted Al and Fe (Al_{0}+1/2Fe_{0}) using various environmental variables and to make soil property maps using a statistical analyses. The soil samples were collected from 321 locations and analyzed to measure the contents of SOM and Al_{0}+1/2Fe_{0}. It was analyzed the relationships among them and various environmental variables such as temperature, precipitation, net primary product, radiation, evapotranspiration, altitude, soil forming energy, topographic wetness index, elevation, difference surrounded area, and distances from the shore and the peak. We can exclude multi-collinearity among environmental variables with principal component analysis and reduce all the variables to 3 principal components. The contents of SOM and Al_{0}+1/2Fe_{0} were estimated by multiple regression models and maps of them were made using the models.

Key words: Soil organic matter, Andic soil property, Volcanic ash soil, Jeju island

Introduction

According to new “Soil Taxonomy” system of the United States Department of Agriculture (USDA), Andisols is defined as soils with Andic soil properties resulted from the presence of significant amount of allophane, imogolite, ferrirydrite, or aluminum-humus complexes. The characteristics of Andic soil properties is related to soil organic carbon, the content of ammonium oxalate extracted Al and Fe (Al_{0}+1/2Fe_{0}), bulk density, and phosphate retention of soils (USDA, 2010).

There have been known 63 types of soils in Jeju Island including volcanic ash soils (Andisols). This diversity was originated from several times of volcanic eruption for a long time, various depths of tephra deposition, and different climatic conditions (Song, 1997). Conventionally, soils in Jeju Island were divided 4 groups of dark brown non-volcanic soils, very dark brown soils, black soils, and forest brown soils in mountain area (Moon et al., 2007). Nowadays, Jeju soils are reclassified using new classification system of Soil Taxonomy by National Academy of Agricultural Science (NAAS), Korea. The contents of soil organic matter (SOM) and Al_{0}+1/2Fe_{0} are important criteria for new soil classification system in the condition of Jeju Island.

Jenny (1941) suggested a state factor theory as a model of dynamic soil system in which soil properties relate to five soil forming factors: climate, organism, topography, parent material, and time. Shoji et al. (1993) also reported the soil forming process of andosolization using the state factor model. Recently, pedometrics, mostly intensified the application of probability and statistics to soil, was applying for predicting soil properties at remote sites for creating and analyzing classifications and exploring multivariate relations (Webster, 1994). Whole quantitative approach is essential to the study and description of soil in pedometrics technology (McBratney et al., 2000).

Therefore, in this study, we conducted to elucidate the distribution of soil properties, the contents of soil organic matter and Al_{0}+1/2Fe_{0}, with pedometrics technology in Jeju Island. We selected some quantitative variables such as mean temperature, precipitation, elevation, and so on, possibly related to static factors, and analyzed their relationships to soil properties with principal component and multiple regression analysis.
Statistical models for estimation of soil organic matter and \( \text{Al}_{0.5} + 1/2 \text{Fe}_0 \) were made using those variables.

**Materials and Methods**

Surface and subsurface soils were collected from 321 locations (Fig. 1). Each site was evenly distributed about 5.8 km² in Jeju Island. Soils were air-dried and passed through 2 mm sieve. The soil samples were analyzed to determine the content of soil organic matter (SOM) by Tyurin method and the content of ammonium oxalate extracted Al and Fe (\( \text{Al}_{0.5} + 1/2 \text{Fe}_0 \)) using a Soil Survey Laboratory method reported by Burt (2004).

We also collected information about environmental variables of the sampling locations from environmental variable maps. Quantifiable environmental information was mean temperature (Temp) and annual precipitation (Rain) as climatic factor, net primary product (NPP), radiation (Rs) and reference evapotranspiration (PMET) as vegetative organism factor, and altitude, topographic wetness index (TWI), net primary product (EEMT), elevation difference surrounded area of 1 km² (EleDiff), Euclidean distance from the shore (Codi) and Euclidean distance from the peak of Mt. Halla (Distfpeak) as topographic factor.

Annual mean temperature map was made by interpolation of inverse distance weighting method with long-term temperature data of 4 weather stations considering lapse rate of temperature along altitude. Precipitation map was made by considering the relationships between altitude and annual precipitation with digital elevation model (DEM) with resolution of 30 m × 30 m.

Net primary product map was made using temperature and precipitation like equation (1) (Grace et al., 2006). Radiation map was made using altitude, maximum and minimum temperatures like equation (2) (Bandyopadhyay et al., 2008). Reference evapotranspiration map was made by Hargreaves method (Hargreaves, 1983) corrected by Penman-Monteith method (Allen et al., 1998; Bandyopadhyay et al., 2008).

\[
NPP = \min(NPP_T, NPP_P) \tag{1}
\]

\[
NPP_T = 3000 \times (1 + \exp(1.315 - 0.0119 \times T))^{0.4}
\]

\[
NPP_P = 3000 \times (1 + \exp(-0.00664 \times P))
\]

\[
T: \text{mean annual temperature(°C)}
\]

\[
P: \text{mean annual precipitation(mm yr}^{-1})
\]

\[
R_s = (1 + 2.7 \times 10^{-5} \times Z) \times K_r \times (T_{\text{max}} - T_{\text{min}})^{0.5} \times R_a \tag{2}
\]

\[
R_s: \text{mean daily solar radiation(MJ m}^{-2} \text{ d}^{-1})
\]

\[
T_{\text{max}}, T_{\text{min}}: \text{maximum and minimum temperature(°C)}
\]

\[
K_r: \text{empirical coefficient(0.16)}
\]

\[
R_a: \text{extraterrestrial radiation(MJ m}^{-2} \text{ d}^{-1})
\]

A map of topographic wetness index was made by a method suggested by Moore et al. (1993) with equation (3). Soil forming energy was considered as effective energy and mass transfer (EEMT) suggested by Rasmussen and Tabor (2007) with equation (4). A map of elevation difference surrounded area of 1 km² (EleDiff) was made by calculating absolute value of difference between mean elevation within 1 km² and elevation of a center cell. The maps of Euclidean distance from the shore and from the peak of Mt. Halla were made by distance calculation method with spatial data.

\[
TWI = \ln(a \tan^{-1} \beta) \tag{3}
\]

\[
TWI: \text{topographic wetness index}
\]

\[
a: \text{local up slope contributing area(m}^2 \text{ m}^{-1})
\]

\[
\beta: \text{slope(degrees)}
\]

\[
EEMT = 347.134 \times 0.5 \times (((T-21.5)/-10.1)^2 +(((P-4412)/1704)^2)) \tag{4}
\]

\[
EEMT: \text{effective energy and mass transfer(MJ m}^2 \text{ yr}^{-1})
\]

\[
T: \text{mean annual temperature(°C)}
\]

\[
P: \text{mean annual precipitation(mm yr}^{-1})
\]
High correlation coefficients among environmental variables show multicollinearity among them at every location (Table 2). Therefore, we conducted principal component analysis (PCA) to eliminate multi-collinearity and reduce environmental variables. The number of variables was determined by Eigenvalue of over one or cumulative explainable value of 0.8. Then we made the linear models to calculate the contents of soil organic matter and $\text{Al}_{0.5}^{+1/2}\text{Fe}_o$ using reduced number of variables with multiple regression analysis.

**Results and Discussion**

Table 1 shows the summary of contents of soil organic matter and $\text{Al}_{0.5}^{+1/2}\text{Fe}_o$ of samples soils at all the locations. Means of soil organic matter contents were 94.3 g kg$^{-1}$ of surface soil, 82.6 g kg$^{-1}$ of subsurface soil, respectively, and means of $\text{Al}_{0.5}^{+1/2}\text{Fe}_o$ contents were 3.29% of surface soil, 3.67% of subsurface soil, respectively. As the contents of $\text{Al}_{0.5}^{+1/2}\text{Fe}_o$, which were considered one of andic soil properties, were high many locations, we considered that many of sampled soils are Andisols.

Table 2 showed the coefficients of correlation between environmental variables. In the table, altitude which showed significant relationships to other variables, has positive relationships to precipitation, radiation, soil forming energy and negative relationships to temperature, net primary products. Temperature and precipitation also have significant relationships to other variables. Many of environmental variables are not independent on other environmental variables, in other words, showed multicollinearity. The multicollinearity among variables causes wrong interpretation of the effect of independent variables on dependent variable. So it should be removed from data for correct interpretation using proper data transformation method (Cha, et al., 2008).

Principal component analysis (PCA) can be used to eliminate multicollinearity (Cha, et al., 2008). With principal component analysis, all the variables, showed

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**Table 1. Statistics of soil organic matter and contents of $\text{Al}_{0.5}^{+1/2}\text{Fe}_o$ at sampled 321 locations in Jeju Island.**

<table>
<thead>
<tr>
<th>Soil layer</th>
<th>Items</th>
<th>Soil organic matter (g kg$^{-1}$)</th>
<th>$\text{Al}_{0.5}^{+1/2}\text{Fe}_o$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>surface soil</td>
<td>mean</td>
<td>94.3</td>
<td>3.29</td>
</tr>
<tr>
<td></td>
<td>std. dev.</td>
<td>65.0</td>
<td>1.96</td>
</tr>
<tr>
<td></td>
<td>minimum</td>
<td>0.1</td>
<td>0.05</td>
</tr>
<tr>
<td></td>
<td>maximum</td>
<td>240</td>
<td>9.22</td>
</tr>
<tr>
<td>subsurface soil</td>
<td>mean</td>
<td>82.6</td>
<td>3.67</td>
</tr>
<tr>
<td></td>
<td>std. dev.</td>
<td>59.6</td>
<td>2.18</td>
</tr>
<tr>
<td></td>
<td>minimum</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td></td>
<td>maximum</td>
<td>230</td>
<td>9.3</td>
</tr>
</tbody>
</table>

**Table 2. Correlation matrix between environmental factors collected at sampled 321 locations.**

<table>
<thead>
<tr>
<th></th>
<th>TWI</th>
<th>TWI</th>
<th>Temp</th>
<th>Rain</th>
<th>ET</th>
<th>NPP</th>
<th>Radiation</th>
<th>EEMT</th>
<th>Codi</th>
<th>DistfPeak</th>
</tr>
</thead>
<tbody>
<tr>
<td>TWI</td>
<td>-0.362</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Temp</td>
<td>-0.983</td>
<td>0.360</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Rain</td>
<td>0.811</td>
<td>-0.362</td>
<td>-0.820</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>ET</td>
<td>0.052</td>
<td>-0.010</td>
<td>0.064</td>
<td>-0.340</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NPP</td>
<td>-0.433</td>
<td>0.019</td>
<td>0.394</td>
<td>-0.041</td>
<td>-0.377</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Radiation</td>
<td>0.610</td>
<td>-0.313</td>
<td>-0.683</td>
<td>0.836</td>
<td>-0.560</td>
<td>0.252</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>EEMT</td>
<td>0.685</td>
<td>-0.341</td>
<td>-0.688</td>
<td>0.971</td>
<td>-0.371</td>
<td>0.078</td>
<td>0.805</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Codi</td>
<td>0.837</td>
<td>-0.261</td>
<td>-0.840</td>
<td>0.696</td>
<td>-0.029</td>
<td>-0.320</td>
<td>0.521</td>
<td>0.623</td>
<td></td>
<td></td>
</tr>
<tr>
<td>DistfPeak</td>
<td>-0.728</td>
<td>0.358</td>
<td>0.655</td>
<td>-0.656</td>
<td>-0.373</td>
<td>0.080</td>
<td>-0.443</td>
<td>-0.622</td>
<td>-0.564</td>
<td></td>
</tr>
<tr>
<td>Elediff</td>
<td>0.767</td>
<td>-0.457</td>
<td>-0.724</td>
<td>0.622</td>
<td>0.177</td>
<td>-0.241</td>
<td>0.475</td>
<td>0.543</td>
<td>0.517</td>
<td>-0.733</td>
</tr>
</tbody>
</table>

* TWI, topographic wetness index; Temp, temperature; Rain, precipitation; ET, reference evapotranspiration; NPP, net primary product; EEMT, soil forming energy; Codi, distance from the shore; DistfPeak, distance from the peak.
Table 3. Eigenvalues and cumulative variance of the correlation matrix of environmental variables.

<table>
<thead>
<tr>
<th>Principal components</th>
<th>Eigenvalue</th>
<th>Proportion</th>
<th>Cumulative</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>6.142</td>
<td>0.558</td>
<td>0.558</td>
</tr>
<tr>
<td>2</td>
<td>2.085</td>
<td>0.190</td>
<td>0.748</td>
</tr>
<tr>
<td>3</td>
<td>1.058</td>
<td>0.096</td>
<td>0.844</td>
</tr>
<tr>
<td>4</td>
<td>0.746</td>
<td>0.068</td>
<td>0.912</td>
</tr>
<tr>
<td>5</td>
<td>0.384</td>
<td>0.035</td>
<td>0.947</td>
</tr>
<tr>
<td>6</td>
<td>0.300</td>
<td>0.027</td>
<td>0.974</td>
</tr>
<tr>
<td>7</td>
<td>0.166</td>
<td>0.015</td>
<td>0.989</td>
</tr>
<tr>
<td>8</td>
<td>0.059</td>
<td>0.005</td>
<td>0.995</td>
</tr>
<tr>
<td>9</td>
<td>0.050</td>
<td>0.005</td>
<td>0.999</td>
</tr>
<tr>
<td>10</td>
<td>0.006</td>
<td>0.001</td>
<td>1.000</td>
</tr>
<tr>
<td>11</td>
<td>0.005</td>
<td>0.001</td>
<td>1.000</td>
</tr>
</tbody>
</table>

Fig. 2. Scatter plot of correlation coefficients between 11 variables and principal components on principal component 1 and principal component 2 axis.

Fig. 3. Scatter plot of correlation coefficients between 11 variables and principal components on principal component 1 and principal component 3 axis.

high correlations among them, can be transformed to the same number of new variables (components) without loss of explain capacity of independent variables. Usually, small number of transformed variables (components) was selected to explain all variation. The selected principal components of all environmental variables were showed in Table 3. The upper three components can explain 84.4% of all variations caused environmental variables.

Scatter plots of component 1 and component 2, and of component 3 and component 4 reveal the relationships among environmental variables (Fig. 2 and Fig. 3). We can name component 1 as “Mountainous effect” which showed the positive relationships to elevation, precipitation, distance from the shore and the negative relationships to temperature, distance from the peak. Component 2 could be named as “Vegetative effect” as it related to net primary product, radiation, evapotranspiration.

Component 3 was difficult to be interpreting, so we named it as “Complex effect”.

The regression model to estimate contents of soil organic matter was made of principal component 1, component 2, and component 3 like equation (5) using multiple regression analysis. This model can be explained 52.4% of all variations of soil organic matter with component 1, 2, and 3. Figure 4 shows the relationship between measured and estimated soil organic matter contents.

\[
\text{SOM} = 9.428 + 1.642 \times (\text{Prin1}) + 1.584 \times (\text{Prin2}) + 0.716 \times (\text{Prin3}) + \varepsilon
\]

SOM: soil organic matter (%)
Prin1: principal component 1
Prin2: principal component 2
Fig. 4. Measured and estimated soil organic matter contents with 3 principal components in surface layer.

Fig. 5. Measured and estimated \( \text{Al}_{\text{o}}+1/2\text{Fe}_{\text{o}} \) contents with 2 principal components in surface layer.

Prin3: principal component 3  
\( \varepsilon \): error

The regression model for \( \text{Al}_{\text{o}}+1/2\text{Fe}_{\text{o}} \) contents was made using only component 1 and 2 in equation (6). This model can explain 38% of total variation of \( \text{Al}_{\text{o}}+1/2\text{Fe}_{\text{o}} \) contents(Fig. 5).

\[
\text{Al}_{\text{o}}+1/2\text{Fe}_{\text{o}}(\%) = 3.289 + 0.324 \times (\text{Prin1}) + 0.624 \times (\text{Prin2}) + \varepsilon
\]  
(6)

\( \text{Al}_{\text{o}}+1/2\text{Fe}_{\text{o}} \): content of ammonium oxalate extracted Al and 1/2Fe(%)  
Prin1: principal component 1  
Prin2: principal component 2

\( \varepsilon \): error

The map of soil organic matter from soil map and estimated map of soil organic matter with model were suggested in Fig. 6. the map of soil organic matter from soil map showed organic matter contents of surface soil. As the results, distribution pattern of soil organic matter in estimated map was very similar to that of soil map. The soils of middle and southeastern regions in Jeju Island have higher contents of soil organic matter in both maps. But there are some different results in detailed parts including mountainous and southwestern area.

Figure 7 showed the map of \( \text{Al}_{\text{o}}+1/2\text{Fe}_{\text{o}} \) contents using equation (6). As the contents of \( \text{Al}_{\text{o}}+1/2\text{Fe}_{\text{o}} \) is one of criteria for Andic soil properties, we can elucidate that most Andisols distributed on middle, eastern, southern parts of island from the map. This result is consistent with the result of Song et al. (1997).

Although models for soil organic matter and \( \text{Al}_{\text{o}}+1/2\text{Fe}_{\text{o}} \) can explain 52% and 38% of all measured variation, respectively, estimated maps are very similar to soil map. So we can suggest the environmental factors are important for soil distribution pattern in
Conclusion

The contents of soil organic matter and \( \text{Al}_{\text{c}}+1/2\text{Fe}_o \) are important criteria for classification of Andisols in new soil classification system. In Jeju Island, there are many types of soils including Andisols. We tried to make the maps of soil organic matter and \( \text{Al}_{\text{c}}+1/2\text{Fe}_o \) using some environmental factors.

Soils were sampled 321 locations in the island and measured the contents of soil organic matter and \( \text{Al}_{\text{c}}+1/2\text{Fe}_o \). The quantitative environmental variables, such as elevation, annual mean temperature, annual precipitation, net primary product, radiation, reference evapotranspiration, soil forming energy, topographic wetness index, elevation difference surrounded area of 1 km\(^2\), Euclidean distances from the shore of the island and the peak of Mt. Halla, were collected. There is multicollinearity among various environmental variables. Using principal component analysis, all the environmental variables were reduced 3 principal components. The first component is interpreted as “Mountainous effect”, the second component as “Vegetative effect”, and the third component as “Complex effect”.

For estimation of soil organic matter content, a regression model was suggested using all 3 principal components. But the contents of \( \text{Al}_{\text{c}}+1/2\text{Fe}_o \) were estimated component 2 and 3. The 52% of variations of soil organic matter and 38% of variation of \( \text{Al}_{\text{c}}+1/2\text{Fe}_o \) could be explained by the regression models. The maps of soil organic matter and \( \text{Al}_{\text{c}}+1/2\text{Fe}_o \) were drawn using regression models, and they are consistent with soil map. We can suggest that environmental factors are important on soil distribution in Jeju Island. It is possible that soil property map can be made using environmental variables and statistical methods.

Acknowledgement

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References


주성분분석 및 다중회귀분석에 의한 제주도 토양유기물 및 \( \text{Al}_0+1/2\text{Fe}_0 \) 함량 분포

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Soil Taxonomy의 새로운 Andisols목 토양의 분류체계에서 토양유기물 함량과 Ammonium oxalate 추출 AI 함량과 Fe의 1/2함량의 합은 중요한 기준이다. 제주도는 토양생성환경이 다양하여 Andisols 토양을 포함하여 다양한 토양이 분포하고 있다. 이 논문은 제주도 토양을 대상으로 기후, 식생, 지형 등 여러 가지 환경변수들을 이용하여 토양유기물과 \( \text{Al}_0+1/2\text{Fe}_0 \)의 함량을 추정할 수 있는 모형을 개발하고, 이를 이용하여 토양특성지도를 제작하기 위하여 수행하였다. 조사대상 지역의 321 지점에서 토양을 채취하여 토양유기물과 \( \text{Al}_0+1/2\text{Fe}_0 \) 함량을 분석하고, 각 토양시료 채취지점의 온도, 강우, 순일차생산량, 일사량, 중반량, 해발고도, 토양생성에너지, 지형습윤지수, 주변과의 고도차, 해안과 지형으로부터의 거리 등의 환경변수들을 환경변수 지도를 제작하여 추출하였다. 여러 환경변수 간에는 서로 상관관계가 높게 나타나는 다중공선성을 나타내었으며, 이를 주성분분석에 의한 변수 변환으로 제거하였다. 주성분분석 결과를 바탕으로 변환된 변수들은 산악효과, 식생효과, 복잡효과 등 3개의 주성분으로 축소할 수 있었고, 이 3개의 변수를 이용하여 토양유기물과 \( \text{Al}_0+1/2\text{Fe}_0 \) 함량을 예측할 수 있는 다중회귀모형을 구하였다. 이 모형들은 전체 토양유기물 변화의 52%와 전체 \( \text{Al}_0+1/2\text{Fe}_0 \) 변화의 37%를 설명할 수 있었다. 모형을 이용하여 제작된 토양유기물 지도는 토양도를 바탕으로 한 토양유기물 지도와 전체적인 형태에서 매우 유사한 형태를 나타내었다. 따라서 환경요인은 제주도 토양의 분포에 큰 영향을 미치는 것으로 판단되었고, 정량화할 수 있는 환경요인을 이용하여 토양특성지도를 제작할 수 있음을 구명하였다.