A PSPICE Circuit Modeling of Strained AlGaInN Laser Diode Based on the Multilevel Rate Equations

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PSPICE circuit parameters of the blue laser diodes grown on wurtzite AlGaInN multiple quantum well structures were extracted directly from the three level rate equations. The relevant optical gain parameters were separately calculated from the self-consistent multiband Hamiltonian. The resulting equivalent circuit model for a blue laser diode was schematically presented, and its modulation characteristics, including the pulse response and the frequency response, have been demonstrated by using a conventional PSPICE.

Keywords: AlGaInN blue LDs, Three-level rate equation, Equivalent circuit, PSPICE

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I. INTRODUCTION

The quaternary alloy AlGaInN has wide band gap energy, varying with the composition and covering almost all the visible spectrum, extending to the ultraviolet region. These nitride semiconductor technologies have led to the development of electrical devices such as optical data storage, mobile communication and medical surgery for applications in high power and high frequency regimes. The blue laser diode (LD) is an important device for such applications, especially for the optical pickup for the Blu-ray disc. An equivalent circuit model of blue LD, once developed, could be directly used in PSPICE for design and analysis of its driver circuitry. Currently available models presented electrical small signal models via RLC circuits including the spontaneous emission and gain saturation [1, 2]. Others presented revised equivalent circuit models to accommodate the two-level and three-level rate equations; one equation explained the continuity of carrier charge in the quantum wells, another described carrier charge in the separate-confinement heterostructure (SCH), and the third recognized the gateway states introduced to connect the carriers in SCH with the carriers in quantum wells [3,4]. In this paper, the PSPICE circuit parameters for blue LDs based on nitride compound semiconductors have been extracted from the three-level rate equations. The relevant optical gain parameters were calculated separately from the self-consistent multiband Hamiltonian equations for the strained multiple quantum well (MQW) LD grown on wurtzite crystals [5]. AlGaInN Blue Laser Diodes are then described by the equivalent-circuit model for the design and analysis using PSPICE. This model provides a stable and accurate way of describing the LD modulation characteristics in both the large- and the small-signal analysis.

II. THE THREE-LEVEL RATE EQUATION AND MODELING EQUIVALENT CIRCUIT

The band structure of the blue LD to be modeled is as shown in FIG. 1. This AlGaInN SCH MQW LD structure is divided into three states for stable and accurate analysis. They are referred to as Separate confinement hetero-structure (SCH) state, Gateway (G) state, and Quantum well (QW) state.
is the optical confinement factor [9]. $\beta$ is the spontaneous emission factor, $G(n_w)$ is the carrier-density-dependent material gain. $v_g$ is the group velocity. Equation (1) denotes that the charge variation in SCH state is the injection current plus transferred carriers from Gateway state to SCH state, minus transferred carriers from SCH state to Gateway state and transferred carriers from SCH state to ground state because of electron-hole recombination. Similarly, equation (2) denotes the charge variation in the Gateway state and equation (3) presents the charge variation in the QW state. This rate equation can be simplified as by Benjamin [10].

$$I_i = \frac{dQ_s}{dt} + \frac{Q_s}{\tau_{gs}} + \frac{Q_G}{\tau_D} - \frac{Q_w}{\tau_{ESC}}. \tag{5}$$

$$\frac{Q_s}{\tau_D} - \frac{Q_G}{\tau_G} = \frac{dQ_{gs}}{dt} + \frac{Q_{gs}}{\tau_{gs}} + \frac{Q_G}{\tau_C} - \frac{Q_{w}}{\tau_{ESC}}. \tag{6}$$

$$\frac{Q_G}{\tau_C} - \frac{Q_w}{\tau_w} = \frac{dQ_{w}}{dt} + \frac{Q_{w}}{\tau_{w}} + \frac{\Gamma q v_g G(n_w)}{\sqrt{1 + \varepsilon_p S}}. \tag{7}$$

$$q \frac{dS}{dt} = \frac{q \Gamma v_g G(n_w) S}{\sqrt{1 + \varepsilon_p S}} - q \frac{S}{\tau_p} + \frac{\beta q v_g G(n_w) S}{\tau_p}. \tag{8}$$

The density of carriers and photons in the three-level rate equations described above are translated into voltages and currents as in Fig. 2. Here $G$ represents the dependent current. $G_1, G_2, G_3, G_4$ are each $\tau_{ss} \cdot Q_S/\tau_s \cdot \tau_D \cdot \tau_{DG} \cdot G_G \cdot \tau_G \cdot Q_G/\tau_G \cdot \tau_G \cdot Q_G \cdot \tau_{SS} \cdot Q_S \cdot \tau_{SS} \cdot Q_S$. The spontaneous photon emission and stimulated photon emission are determined by the dependent current source $G_{spon}$ and $G_{stim}$, respectively

$$G_{spon} = q \Gamma v_g G(n_w) V_{spon}, \quad R_p = \frac{\tau_p \bar{p}}{q}, \quad C_p = \frac{q}{\bar{p}}. \tag{9}$$

$$V_{spon}(V) = P_{spon}(W) = p S, \quad \bar{p} = \frac{1}{2} \frac{h v_g}{L_i} \frac{1}{R}. \tag{10}$$

Where $\bar{p}$ is a constant for converting photon population. $\varepsilon_p$ is the gain suppression factor for nonlinear

G : Dependent current source
E : Dependent voltage source

FIG. 2. PSPICE equivalent circuit model derived from the three-level rate equations.
optical gain properties. This nonlinear gain factor is partially caused by the depletion of electrons at certain energy levels due to strong stimulated recombination. \( h \) is Planck’s constant, \( L \) is the cavity length, and \( R \) is the end-face reflectivity [10].

III. BLUE LASER DIODE PARAMETER EXTRACTIONS

The 405 nm laser diode under investigation has typical AlGaInN MQW active structures as shown in FIG. 3. The quantum well regions are 3 nm In_{0.12}Ga_{0.88}N and the barrier regions are In_{0.02}Ga_{0.98}N. The SCH regions are Al_{0.2}Ga_{0.8}N and the cladding regions are N- and P-doped Al_{0.13}Ga_{0.87}N sandwiched by GaN ohmic contact layers [11].

FIG. 4. shows the energy band diagram of multiple quantum well (MQW) and electron blocking layer (EBL). For the enhanced optical performance, P-doped Al_{0.3}Ga_{0.7}N EBL is indispensable for the suppression of electron overflow from the active layer to the p-type cladding layer. The gain and spontaneous emission spectra of the AlGaInN QW LD are obtained by a numerical analysis of self-consistent Poisson equations and the Hamiltonian equations for multiband strained wurtzite multiple quantum well structures [12].

FIG. 5 shows gain spectra for the various carrier injections from \( 1.8 \times 10^{19} \text{ cm}^{-3} \) to \( 5.0 \times 10^{19} \text{ cm}^{-3} \) in 20 steps. FIG. 6 shows the variation of maximum material gain (\( G_{\text{max}} \)) and the differential gain (\( G_N \)) due to carrier density.

The gain was calculated using the \( k \)-selection rule, taking into account the intraband relaxation broadening. An excellent fit to the results can be obtained with the following expression [4, 5].

\[
G(n_w) = G_0 \times (n_w - G_1) + G_2.
\]

where \( G_0 \) is the optical-gain coefficient and \( G_1, G_2 \) are the carrier density for transparency [13]. Other parameters were also extracted by following the procedures described in as shown in TABLE 1. [3-14].

![FIG. 3. Schematic perspective of the AlGaInN MQW LD.](image)

![FIG. 4. Band profiles of the MQW and EBL regions obtained by the self-consistent analysis.](image)

![FIG. 5. Gain spectra for the various carrier injections from \( 1.8 \times 10^{19} \text{ cm}^{-3} \) to \( 5.0 \times 10^{19} \text{ cm}^{-3} \) in 20 steps.](image)

![FIG. 6. Maximum material gain (\( G_{\text{max}} \)) and Differential Gain (\( G_N \)) of AlGaInN MQW LD.](image)
IV. SIMULATION RESULTS AND DISCUSSION

The simulation results show full characteristics of blue LD in small-signal and large-signal regimes. First, the pulse response was shown in FIG. 8, where it shows the existence of a few ns turn-on delay and a relaxation oscillation when increasing the pulse signal. The damping of the oscillations, determined by the gain suppression factor, can also be recognized.

The frequency response characteristics of the blue LD are also shown in FIG. 9 and FIG. 10 for two different values of the gain suppression factors. Both the figures show the increase of the 3dB bandwidth according to the optical power increase. Furthermore, the maximum peak values of the responses are decreased by increasing the optical power. Such a characteristic behavior in the frequency response has been predicted elsewhere which takes into account the presence of gateway states [4, 6]. FIG. 11 shows the effect of the gain suppression factor on the modulation characteristics, which shows a decrease in the modulation bandwidth due to the over damping [4, 15].

The V-I characteristics curve for equivalent circuit
model of Blue LD are shown in FIG. 12. This figure shows that the threshold current of blue LD is 60 mA.

V. CONCLUSION

In this work, the modulation characteristics of AlGaInN blue laser diodes were described by an equivalent-circuit model for the conventional PSPICE. This model is based on the three-level rate equations that include the role of gateway states at the quantum well in their characterization of charge dynamics. The device parameters were extracted from the optical gain properties of the MQW active region using the self-consistent Poisson equation and the multiband Hamiltonian for the strained wurtzite crystal. The resulting model is schematically presented and the modulation characteristics were proved by using the convention SPICE, which shows all the key features expected in MQW LD operation such as modulation bandwidth dependence on injection current and turn-on delay, the relaxation oscillation, as well as the over damping effect due to the gain suppression. Such an equivalent circuit model is expected to be directly applicable for optical data storage, mobile communication and medical machinery.

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